

JET PHYSICS

2012 Cargese summer school

August 25, 2012

Matthew Schwartz
Harvard University

Outline

- Lecture 1: Jets and QCD
 - The physics of jets
 - Including brief history
 - Jets from perturbative QCD
 - Jet algorithms
 - Some data
- Lecture 2: Modern jet physics
 - Jet substructure
 - Jet grooming
 - Jet properties
 - The future of jets

THE PHYSICS OF JETS

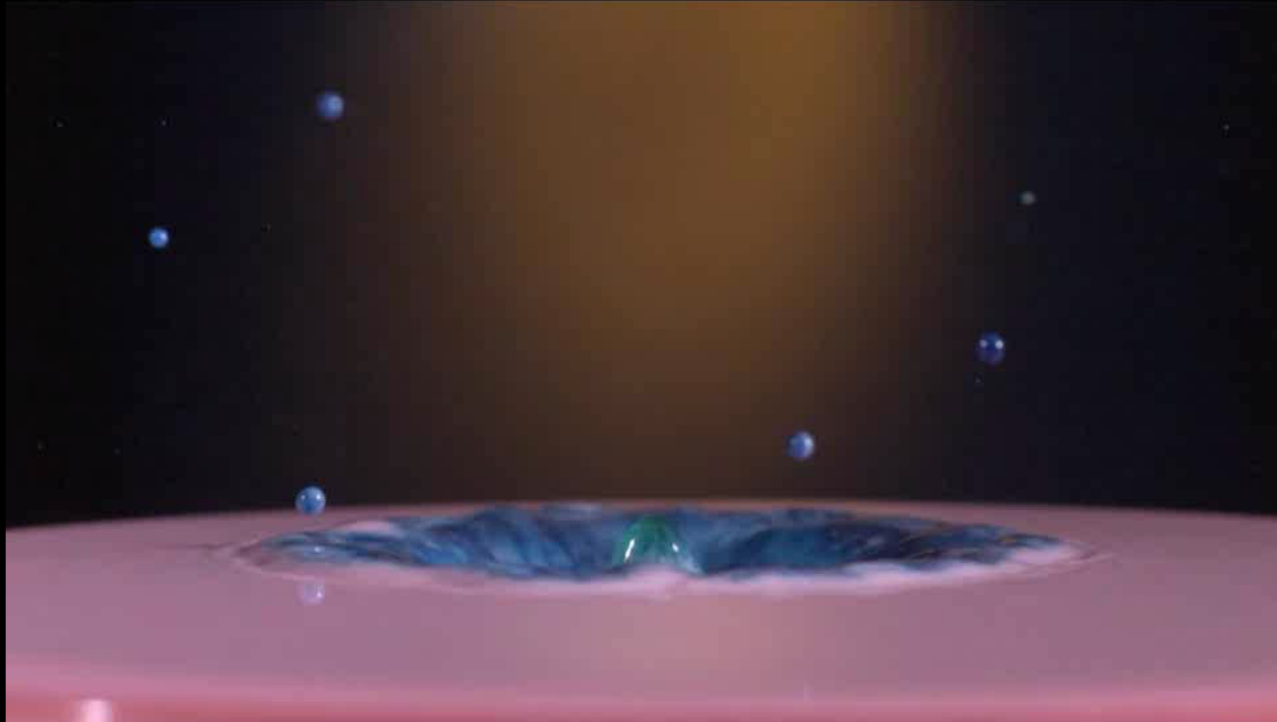
What happens in a collision?

Colliding water droplets – what happens?



What happens in a collision?

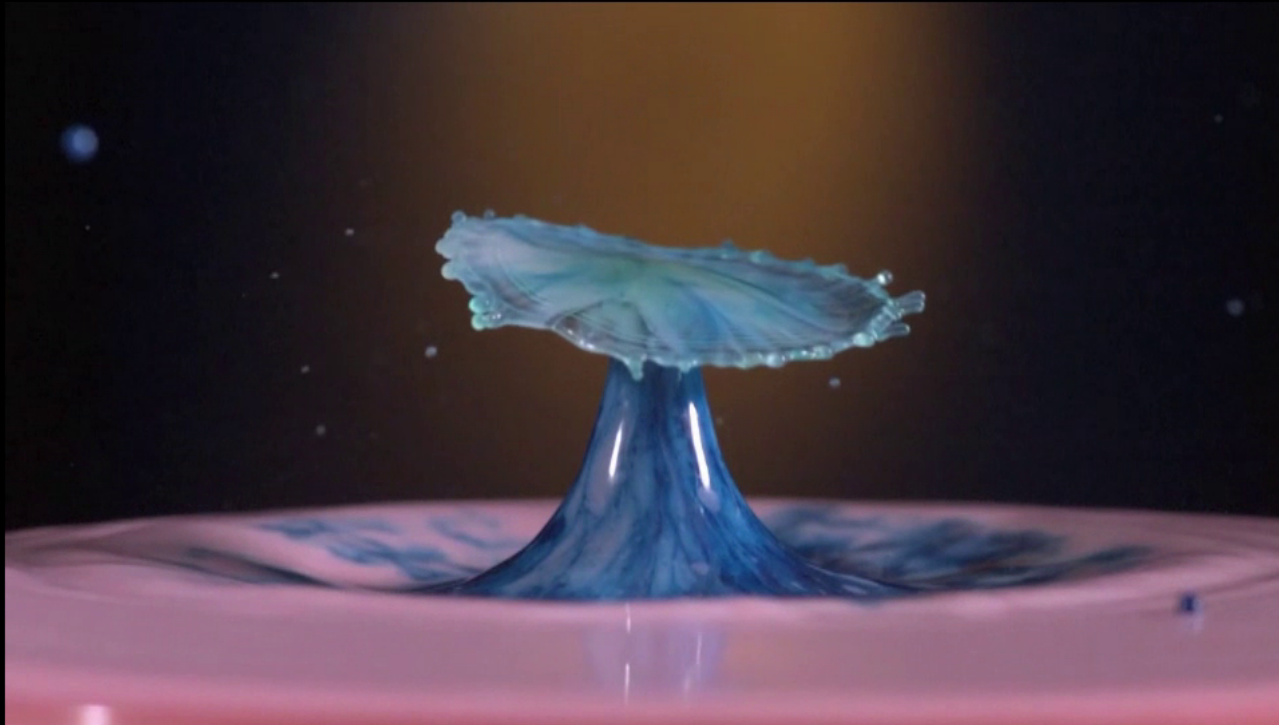
Colliding water droplets – what happens?



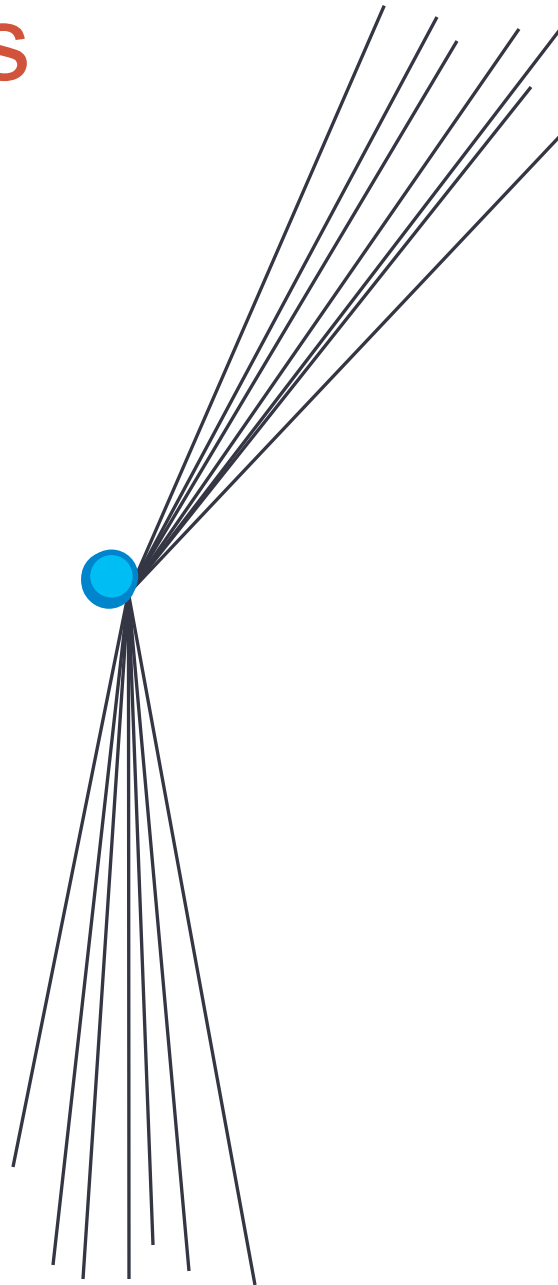
What happens in a collision?

Colliding water droplets – what happens?

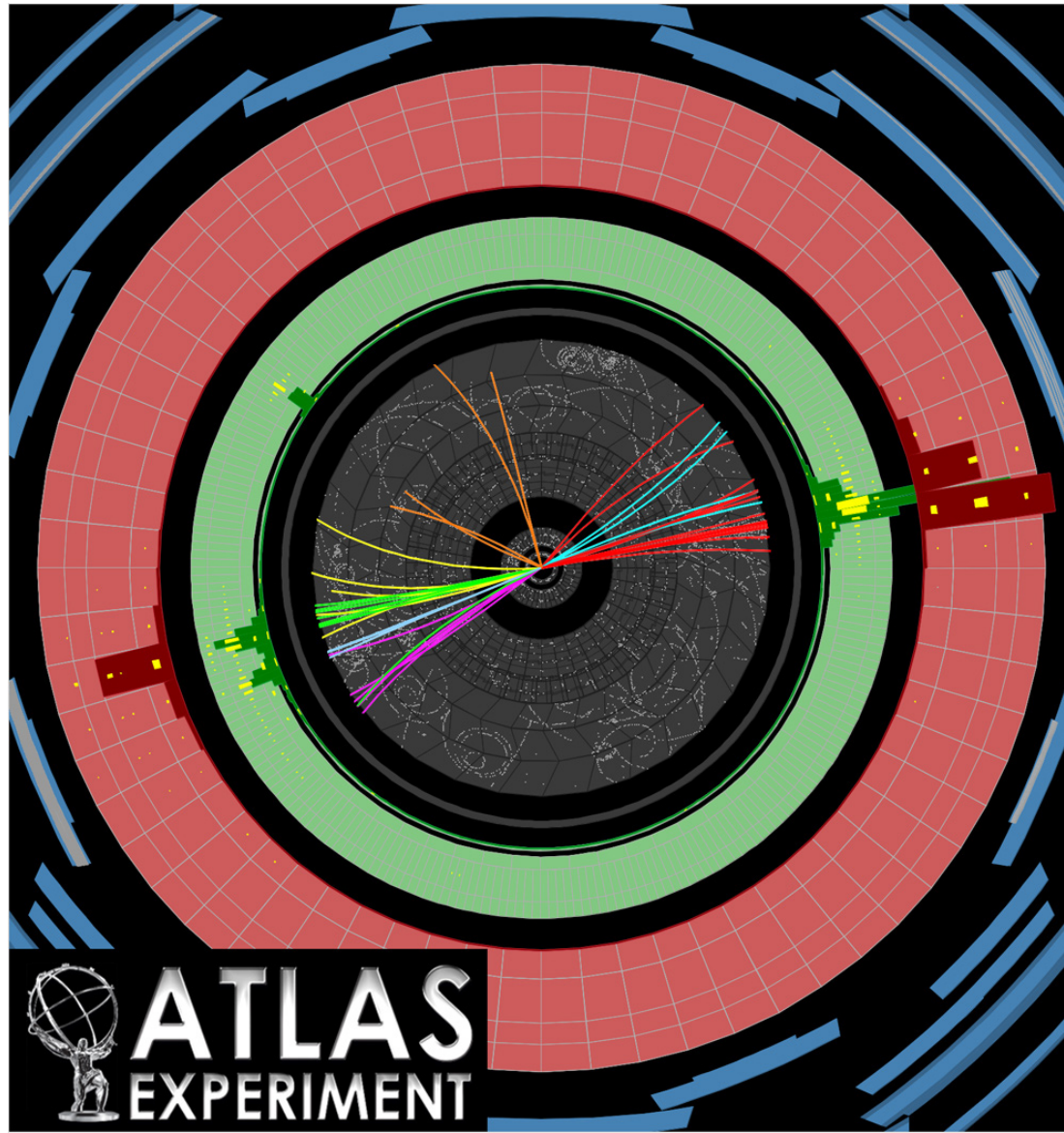
Produces **radially symmetric** distribution



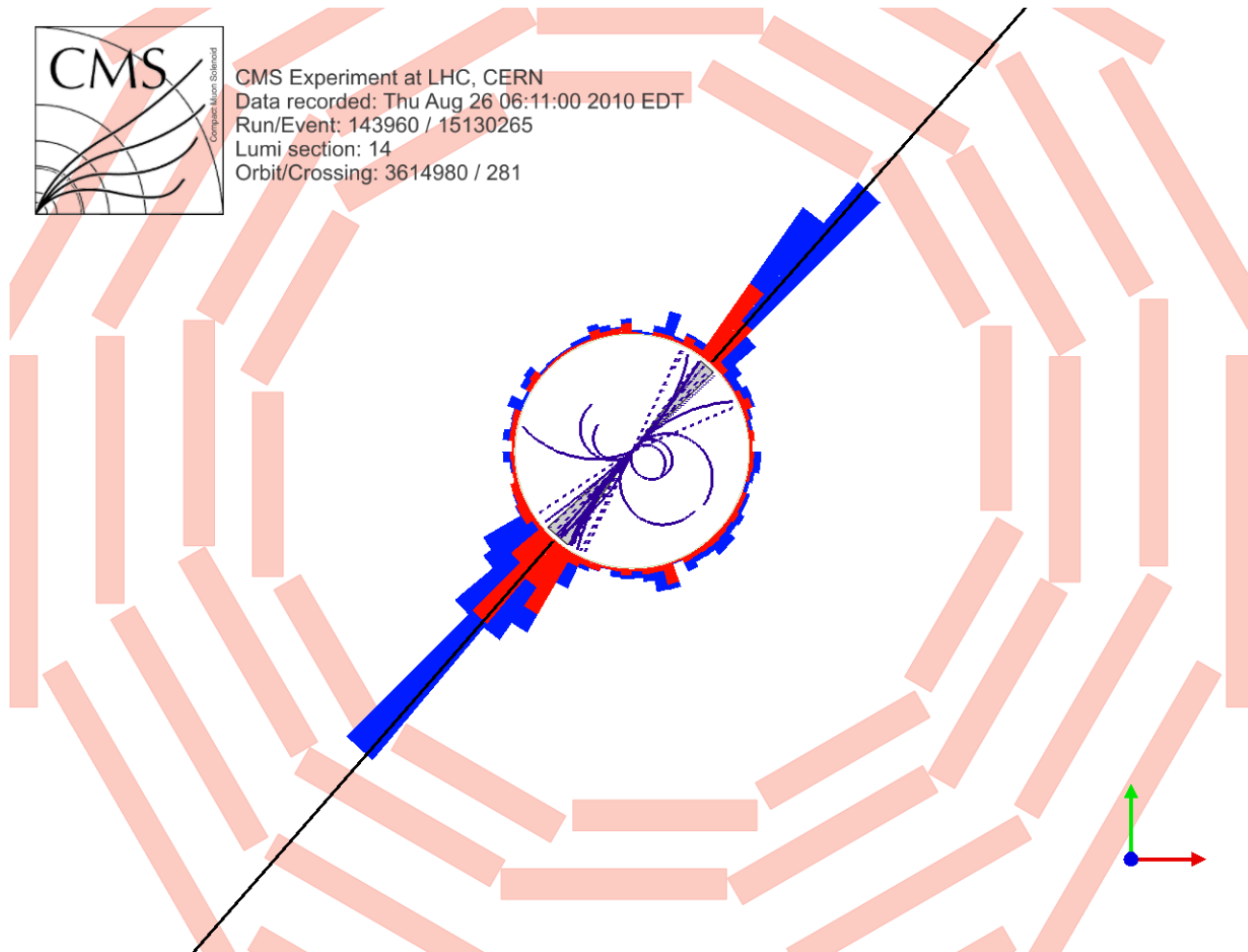
Colliding protons



Colliding protons



Colliding protons



Jets and the LHC

- The LHC has much **higher energy** than any collider ever
 - **More** jets
 - **Harder** (more energetic) jets
 - More **jet-like** (collimated) jets
- LHC experiments can **measure** jets **really well**
 - Better **energy resolution** than Tevatron
 - Better **spatial resolution** than Tevatron
 - Can identify individual particles!!

Jet physics is entering a **Golden Era**

Revolution in the last 4 years

New experimental
techniques

New ideas
and algorithms

New theoretical
methods

BRIEF HISTORY

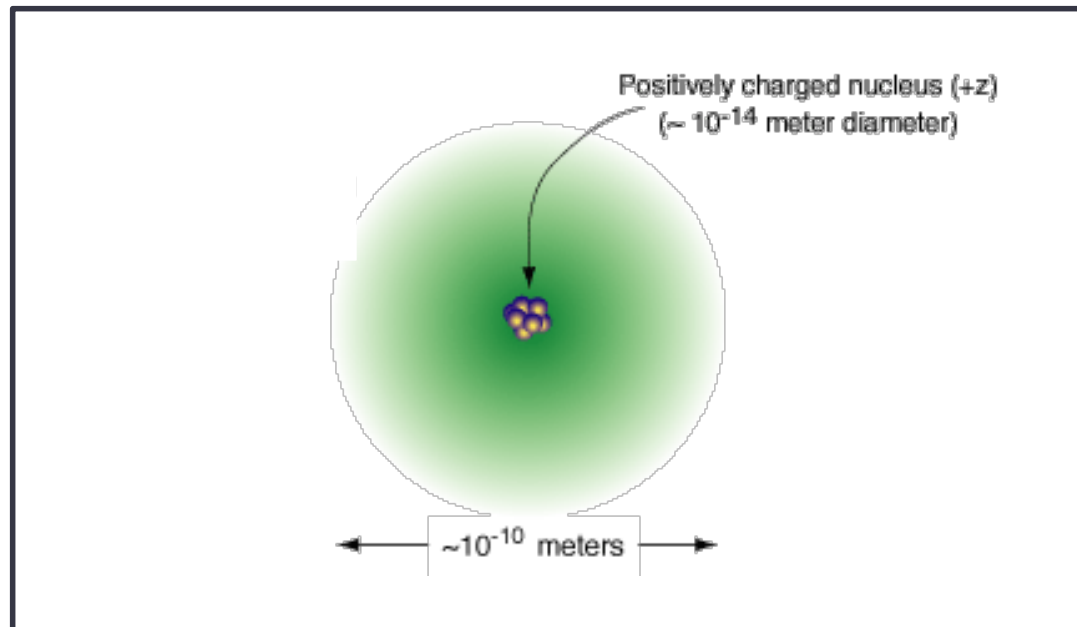
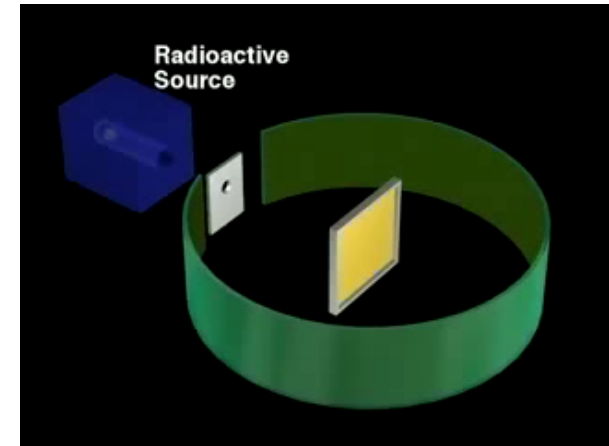
Nuclear physics begins

Rutherford's Experiment (1910)

- α particles from ^{214}Po on $0.5\ \mu$ thick sheet of gold
- α particle speed = 10^7 m/s

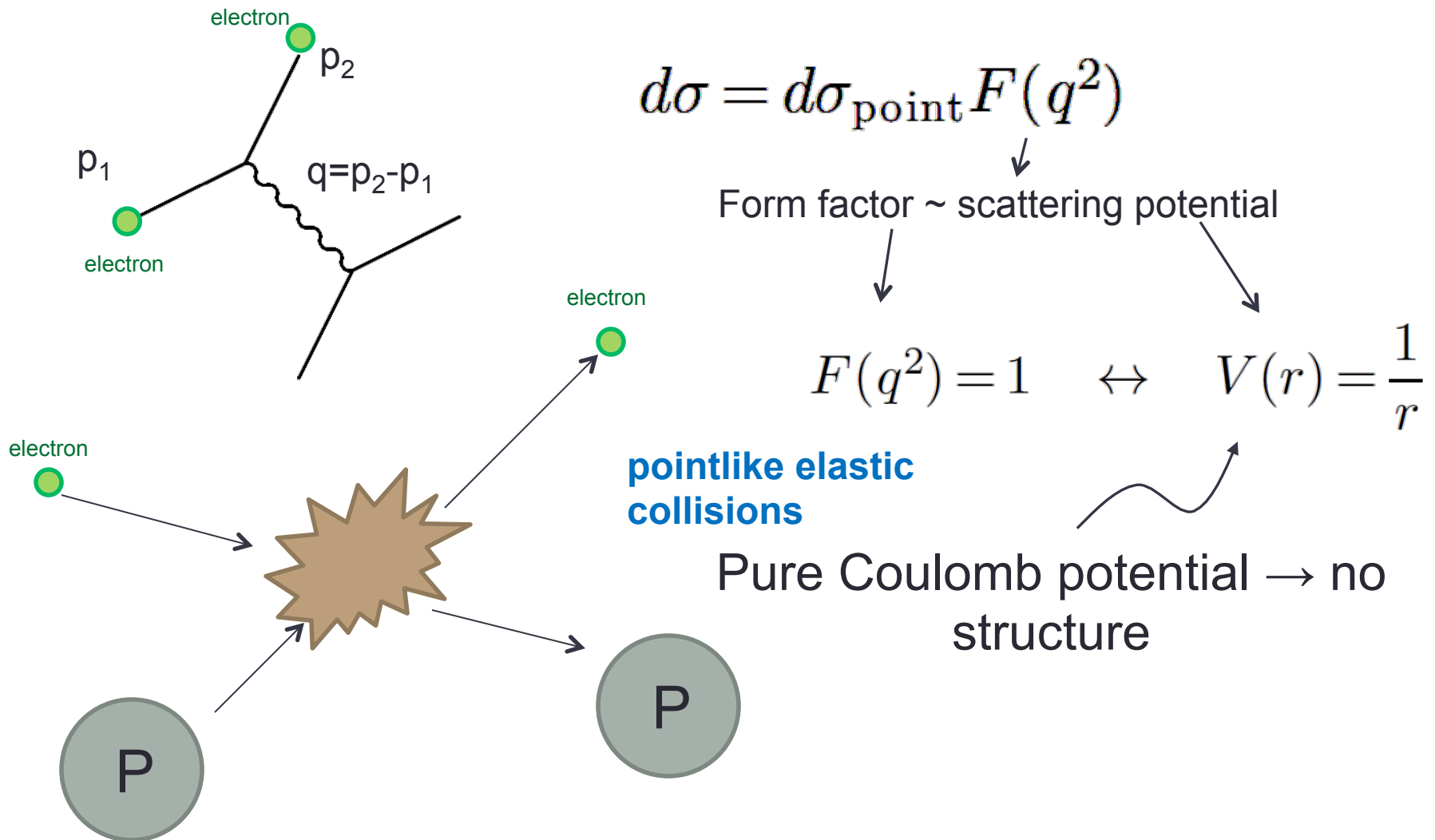
Rutherford concluded:

- Most of the gold foil is **empty space**
- Mass is concentrated in a **hard central nucleus**
- Size of nucleus is approximately 3×10^{-14} m (very close to correct)



Electron-positron ($e^- P^+$) scattering

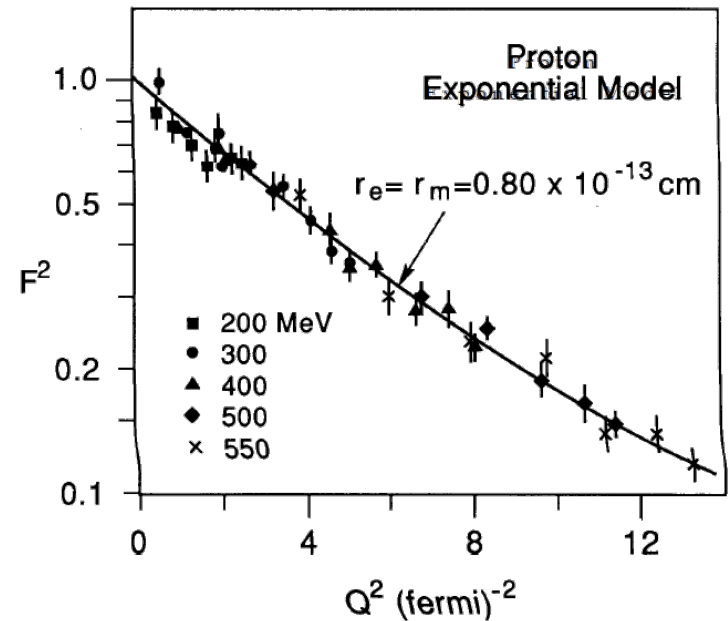
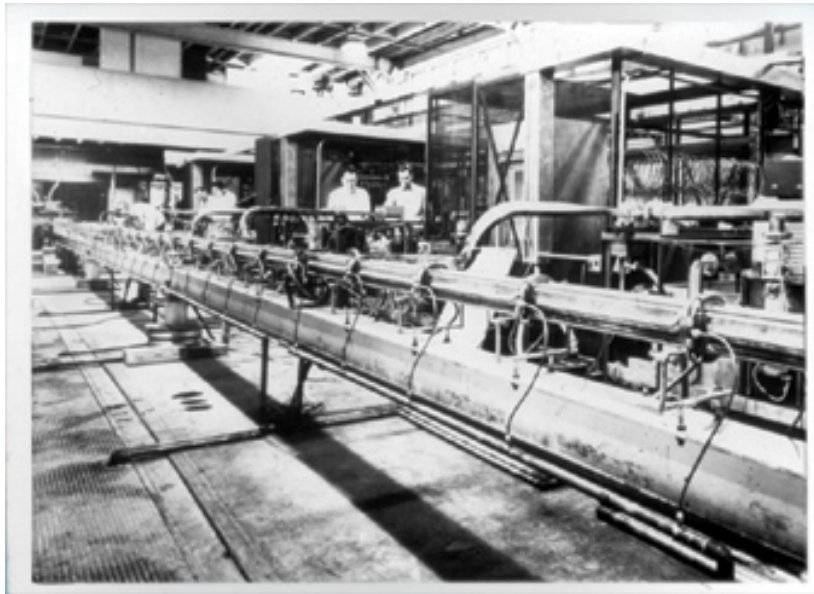
In general, the cross section depends on the momentum transfer q^2



Electron-positron ($e^- P^+$) scattering

1950s at the Mark III linear collider at Stanford

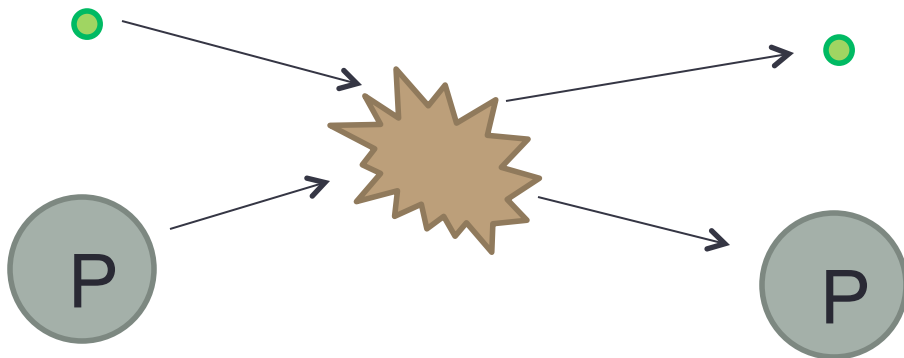
- Energies of order 200-500 MeV



$$F(q^2) \sim \frac{1}{1 + \left(\frac{q}{0.71 \text{ GeV}}\right)^2}$$

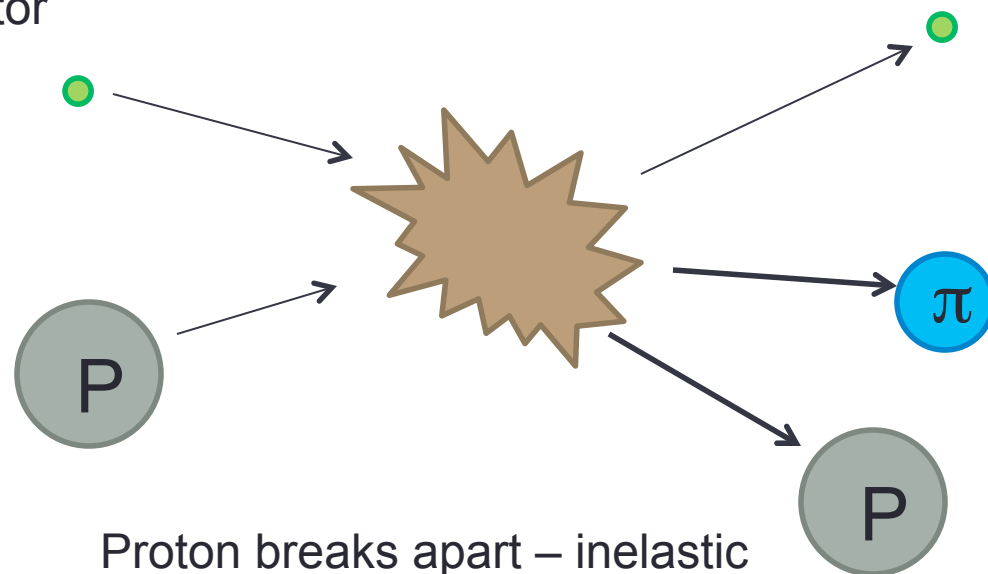
$$\Leftrightarrow V(r) = \frac{1}{r} e^{-(0.7 \text{ GeV})r}$$

Proton has size: $r = 10^{-15} \text{ m}$



Higher energy $e^- P^+$ scattering

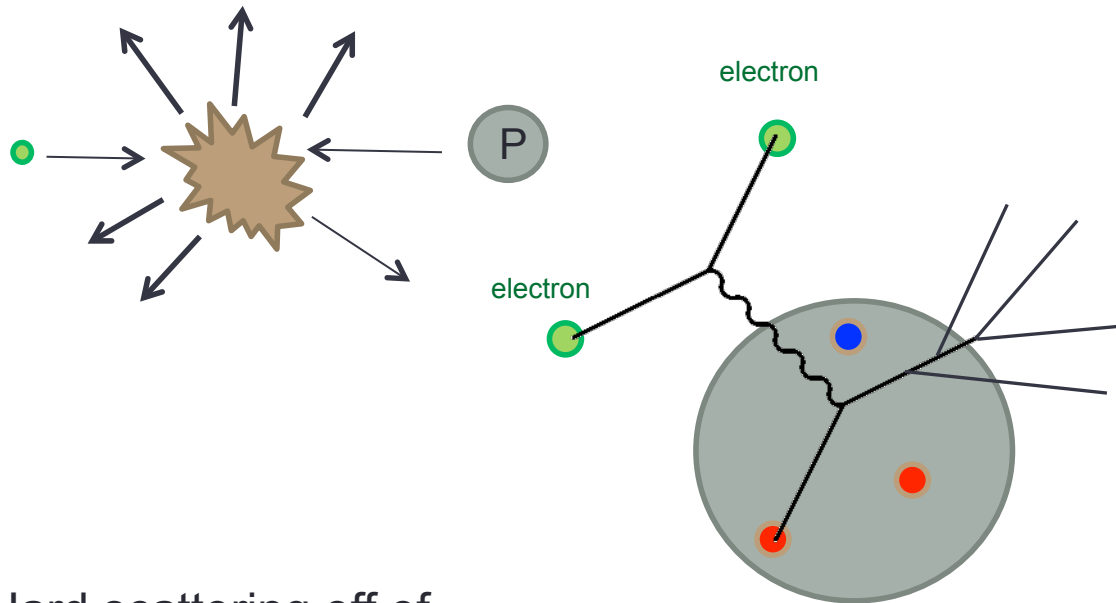
1960s at Stanford Linear Accelerator
(SLAC)



Proton breaks apart – inelastic scattering!

Very high energy $e^- P^+$ scattering

1960s at SLAC



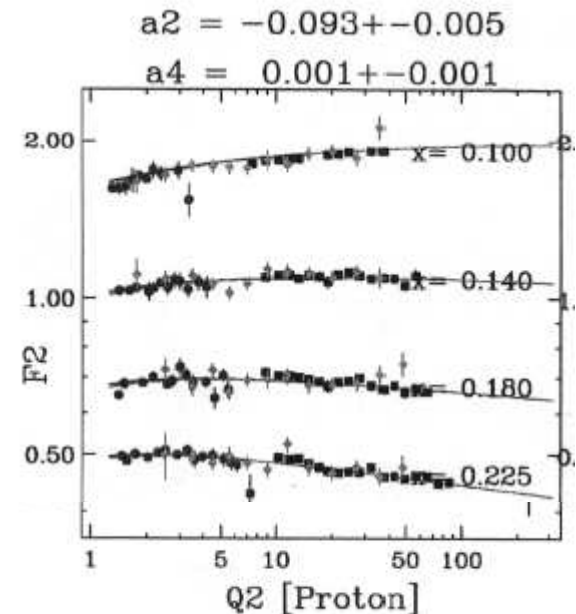
Hard scattering off of
pointlike weakly interacting **constituents** in the proton

quarks

What happens to the proton?

Hard to tell -- DIS experiments of the 50s and 60s were **fixed-target** experiments

-- not designed to measure the “hadronic” part, **just the electron**

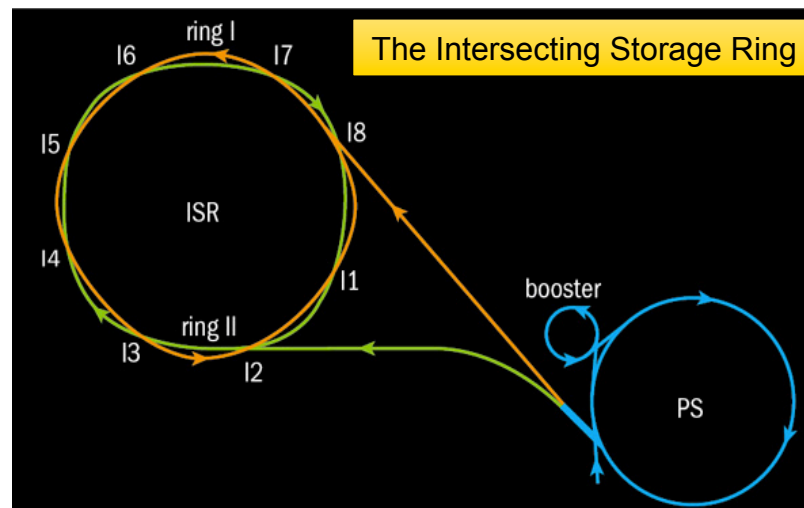
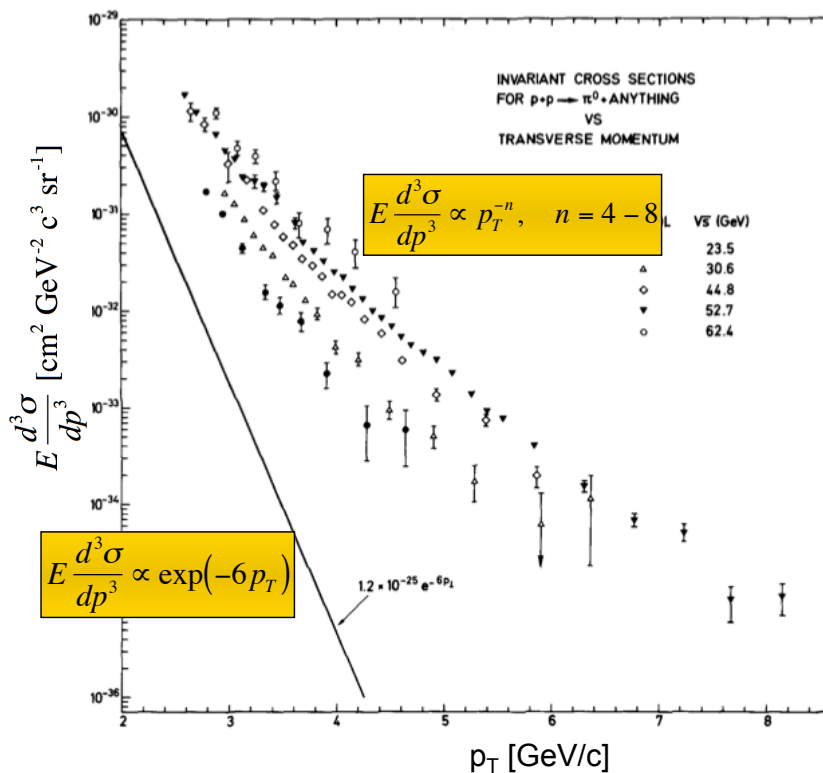


Now $F(q^2) = \text{constant}$ again!

Intersecting Storage Rings (ISR) at CERN

First hadron (pp) collider

From T. Schörner-Sadenius



- Unexpected **rise** in the total **pp cross section**
- Large number of particles produced at **high p_T**
- Consistent with (early) expectations from QCD

Spear at SLAC

Mark I -- first 4π detector (1973-1977)

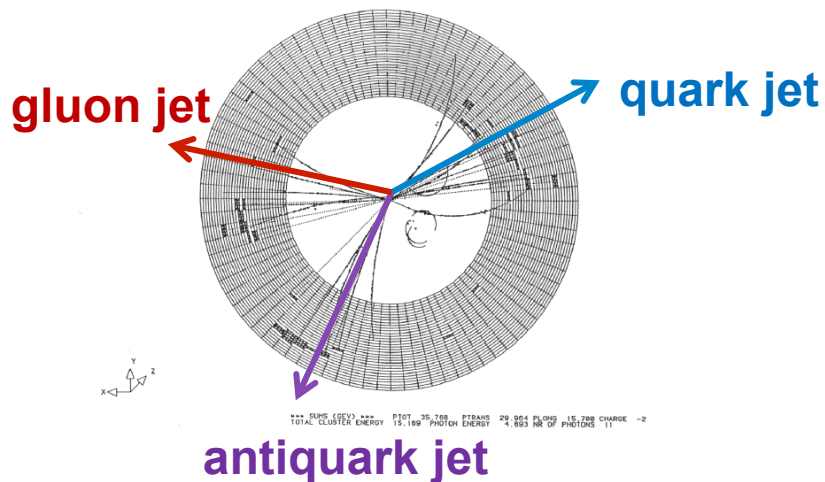
- Confirmed jet models with event shapes

$$S = \frac{3\left(\sum_i p_{T,i}^2\right)}{2\left(\sum_i p_i^2\right)}$$

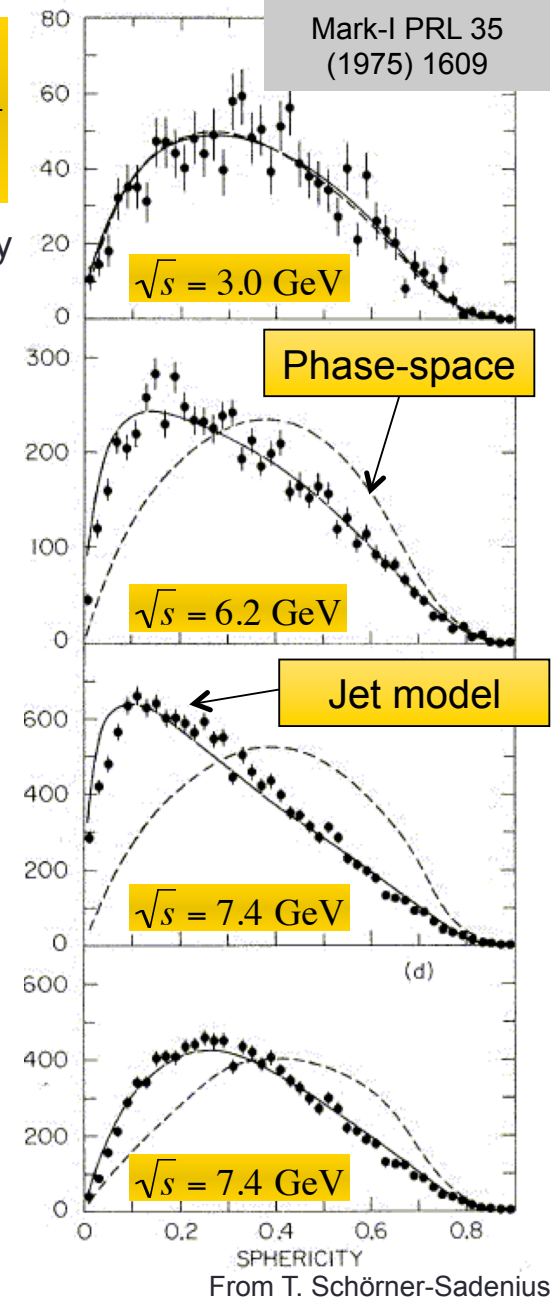
Measured Sphericity
(event shape)

PETRA at DESY (Hamburg)

Gluon jets

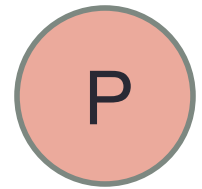
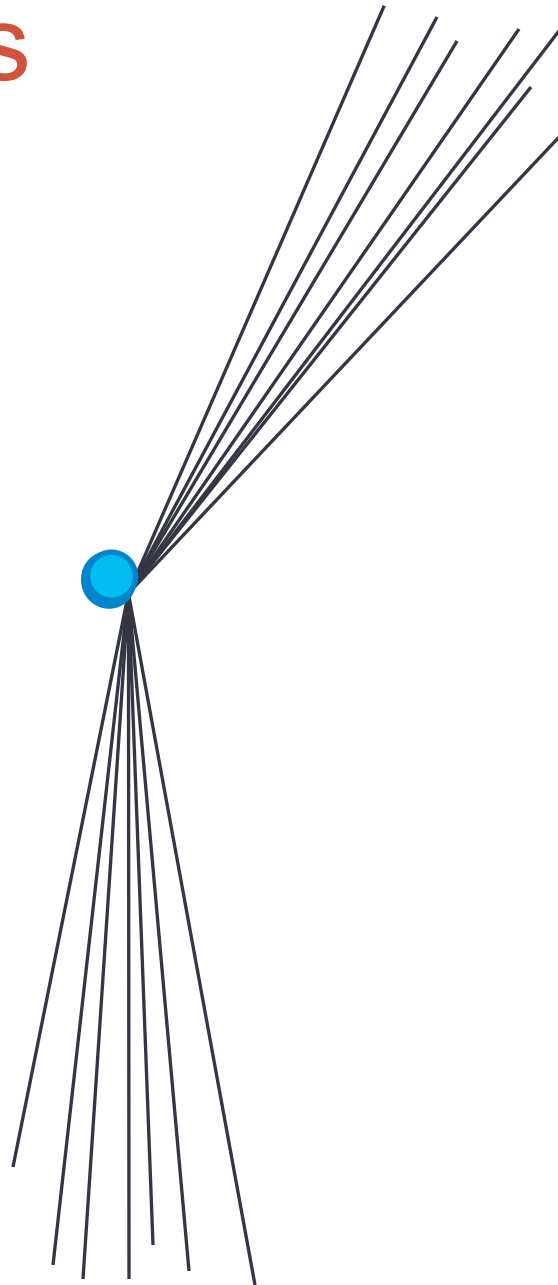
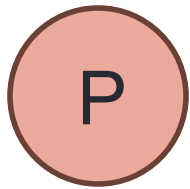


PETRA (DESY) 1979

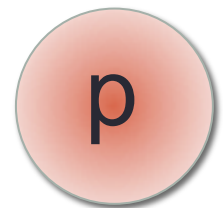
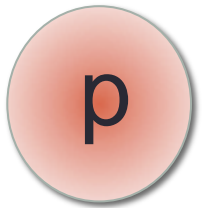


THE PHYSICS OF JETS

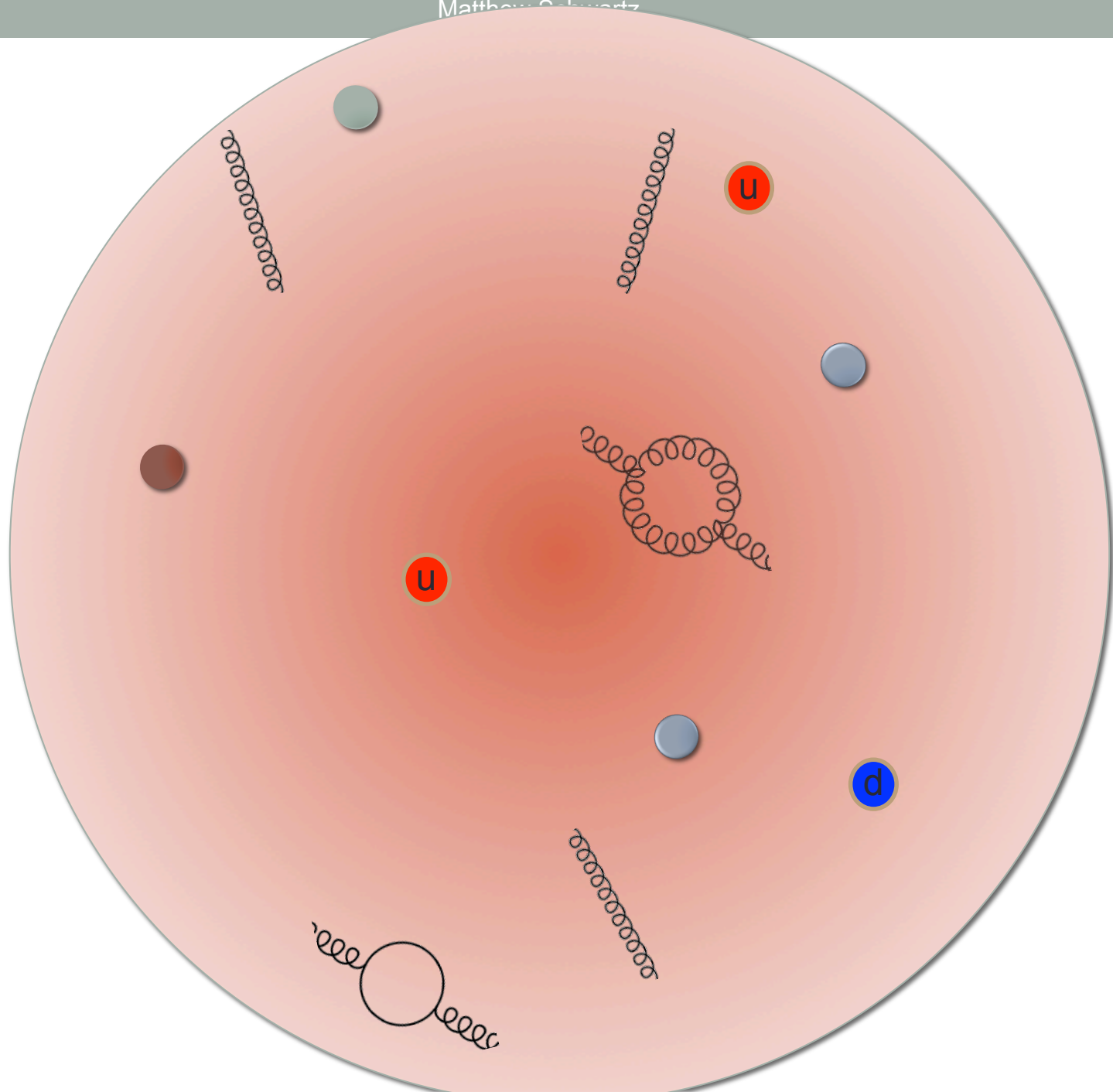
Colliding protons

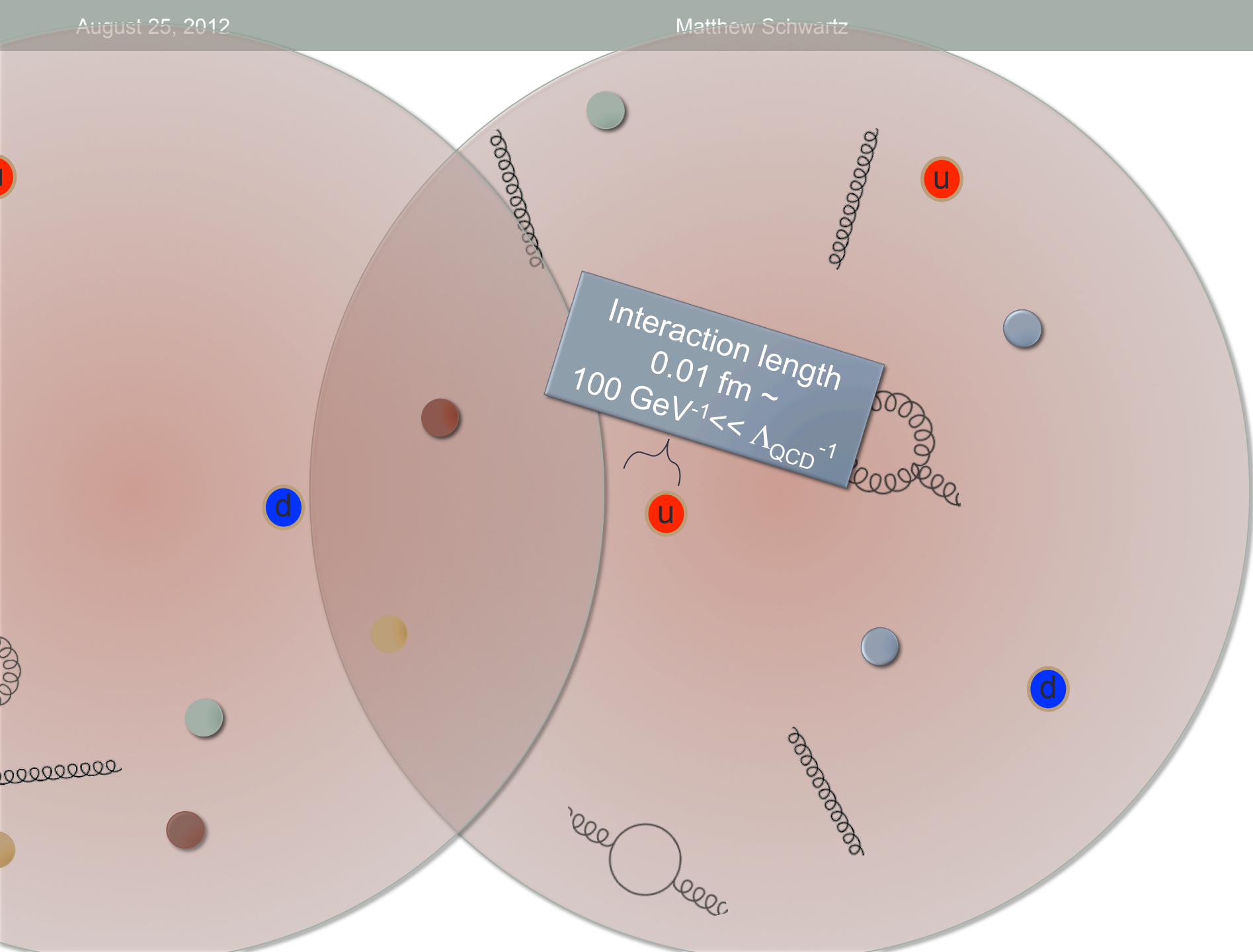


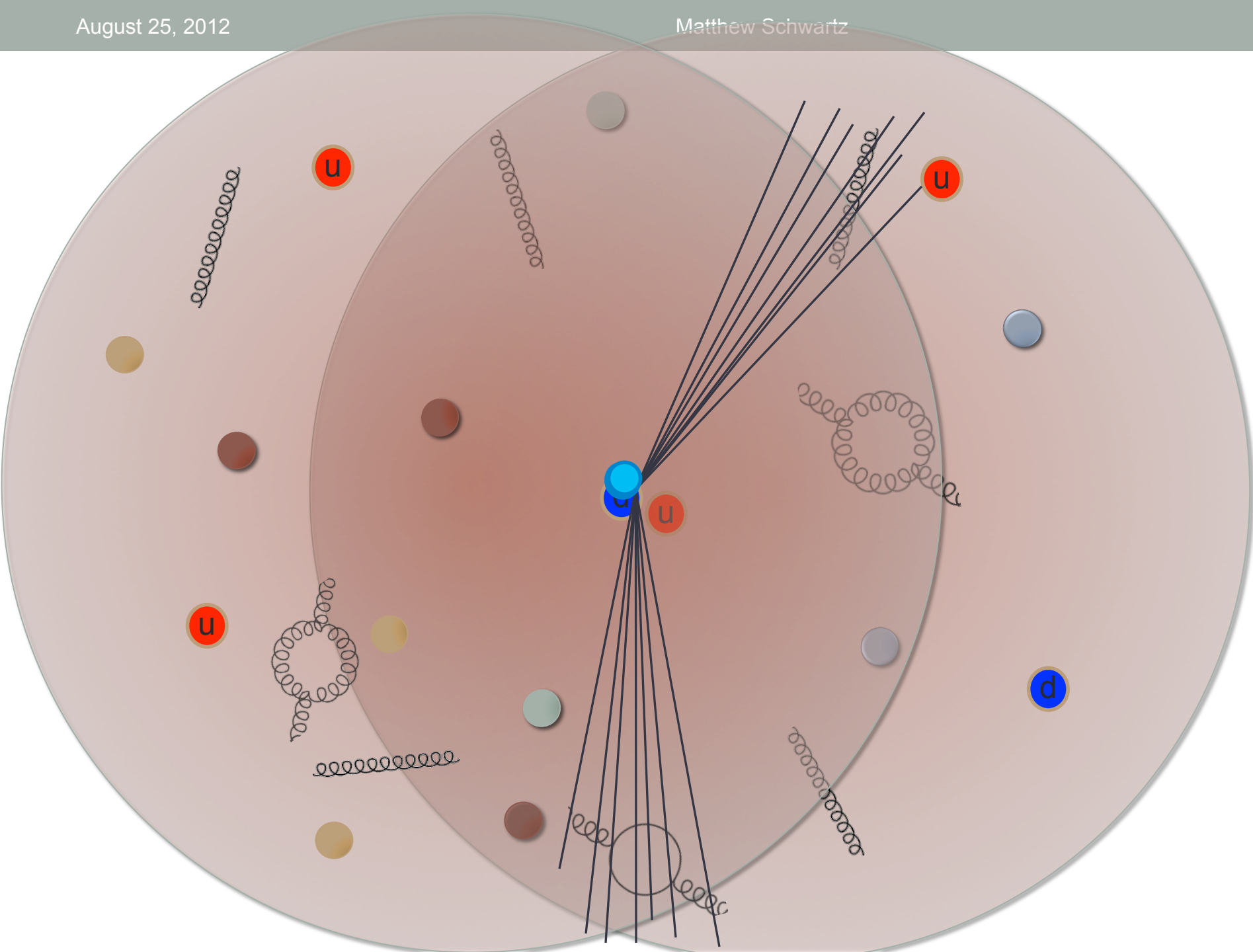
Colliding protons



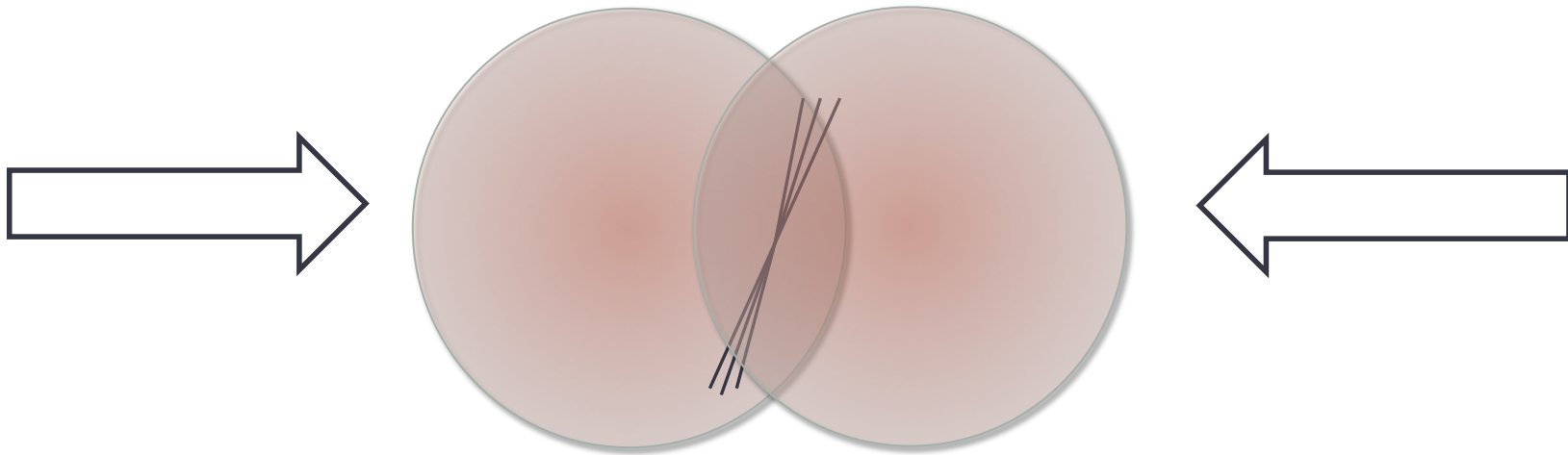
Size is
 $1 \text{ fm} \sim \Lambda_{\text{QCD}}^{-1}$



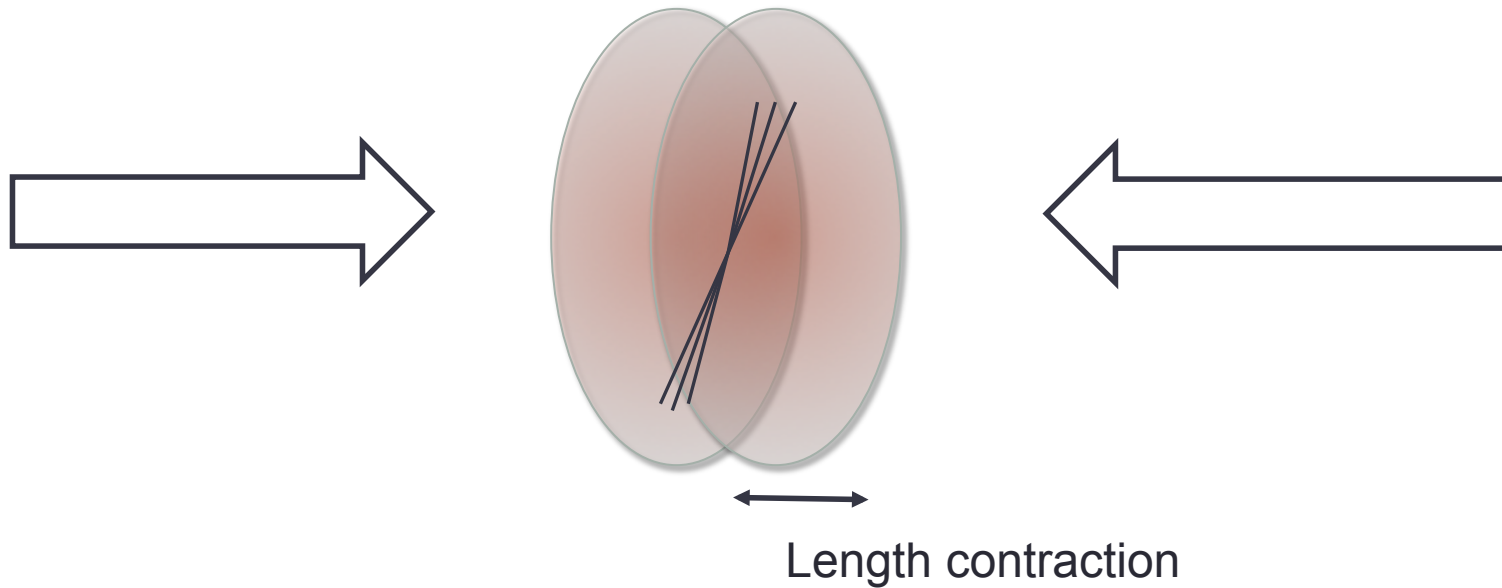




Special relativity



Special relativity

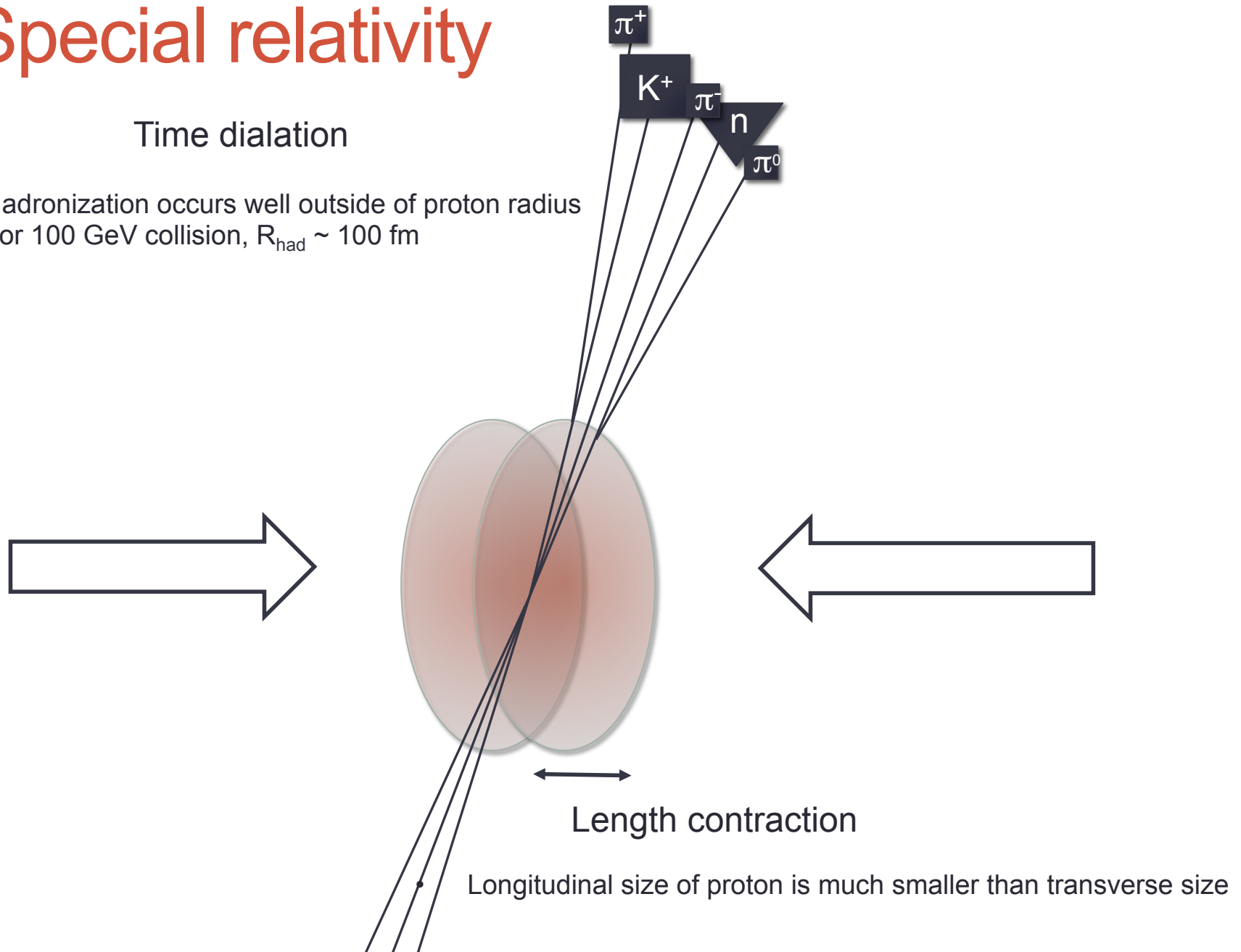


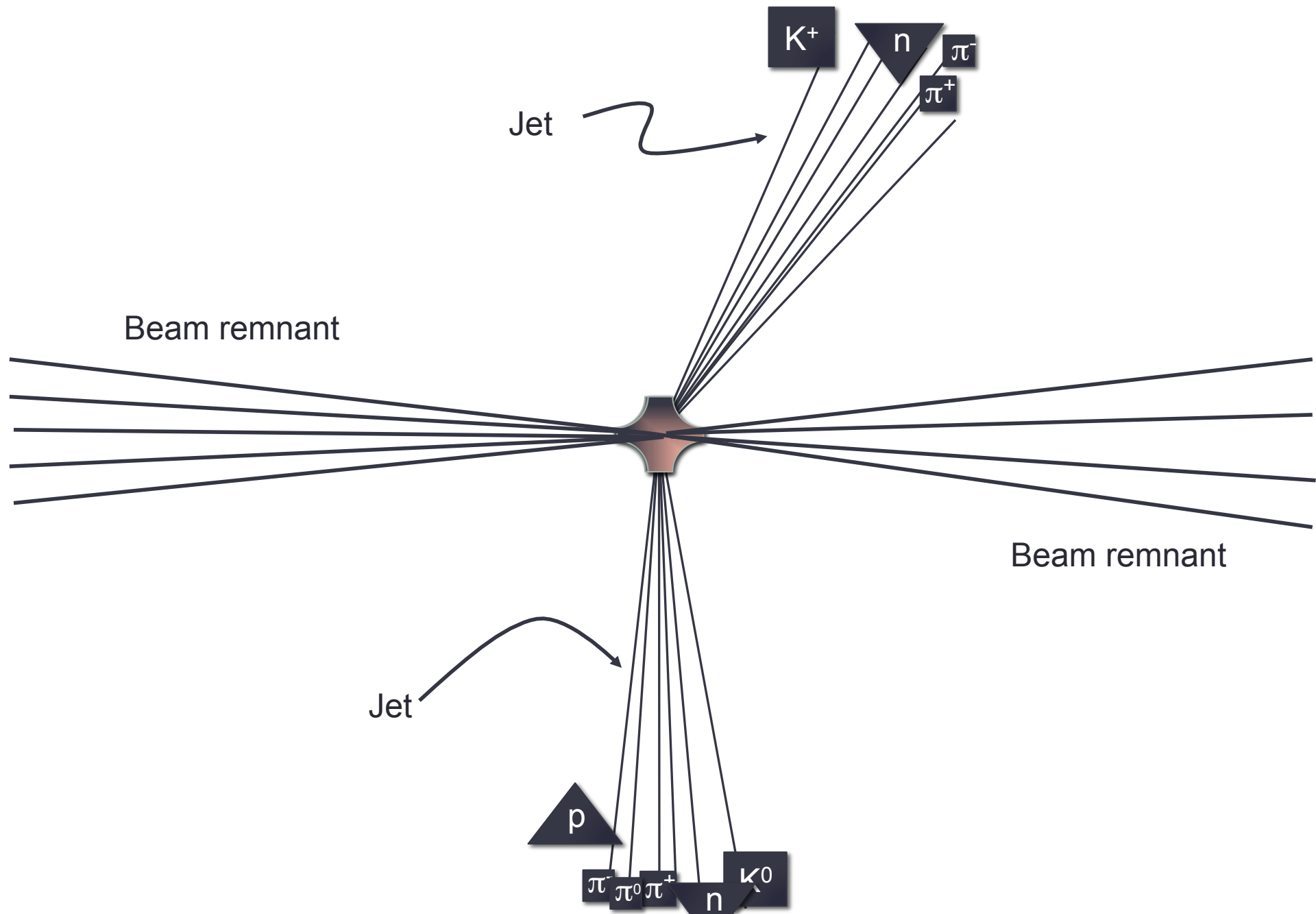
- Longitudinal size of proton is much smaller than transverse size

Special relativity

Time dialation

- Hadronization occurs well outside of proton radius
- For 100 GeV collision, $R_{\text{had}} \sim 100 \text{ fm}$

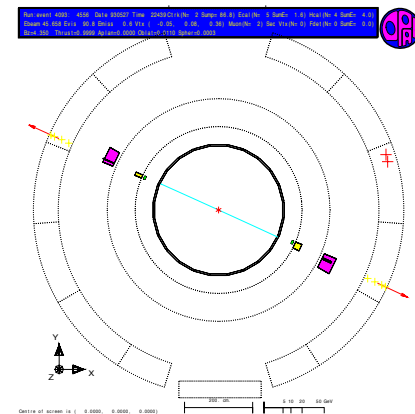
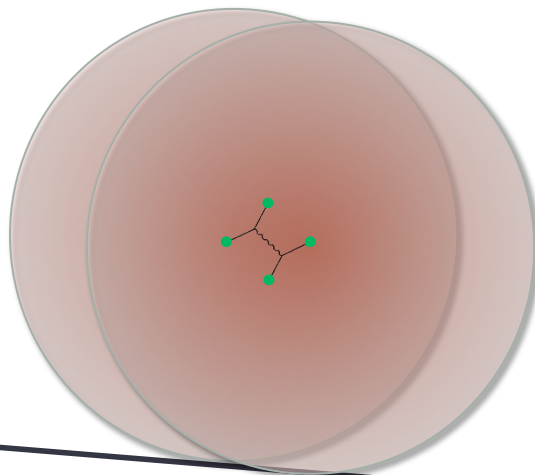




at **short distances**

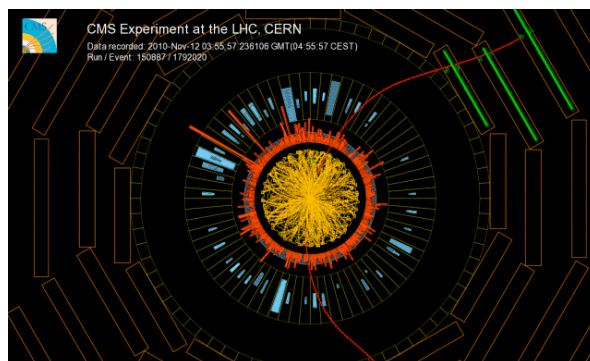
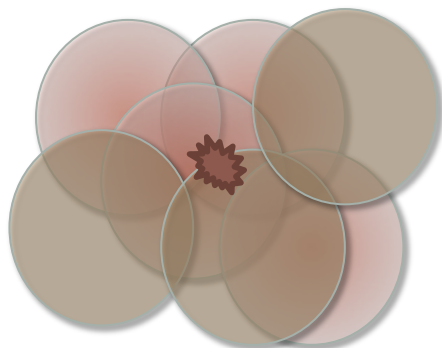
QCD is like QED

- Electrons in, electrons out



at **long distances** QCD is a mess

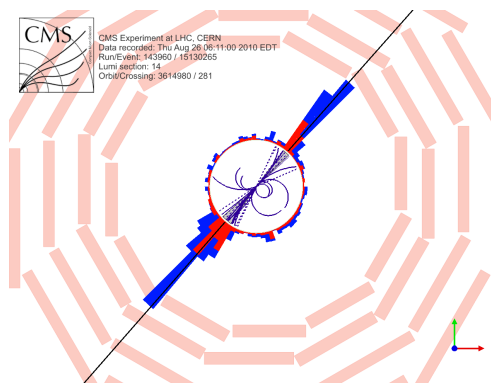
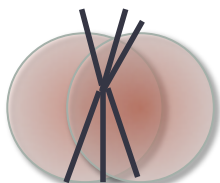
- Nuclei in, hadrons out



OPAL $e^+e^- \rightarrow \mu^+\mu^-$ event

CMS
Heavy ion event

Proton-proton collisions are just right
intermediate between QED and a mess



CMS
Dijet event

QCD predicts jets

1. Quarks and gluons (partons) are produced at short distance, \longrightarrow Production
2. As they propagate outward, they radiate more partons \longrightarrow Radiation
3. At distances $\sim \Lambda_{\text{QCD}}^{-1}$ they form uncolored hadrons \longrightarrow Hadronization
Hadrons leave the proton and do not interact strongly until detected

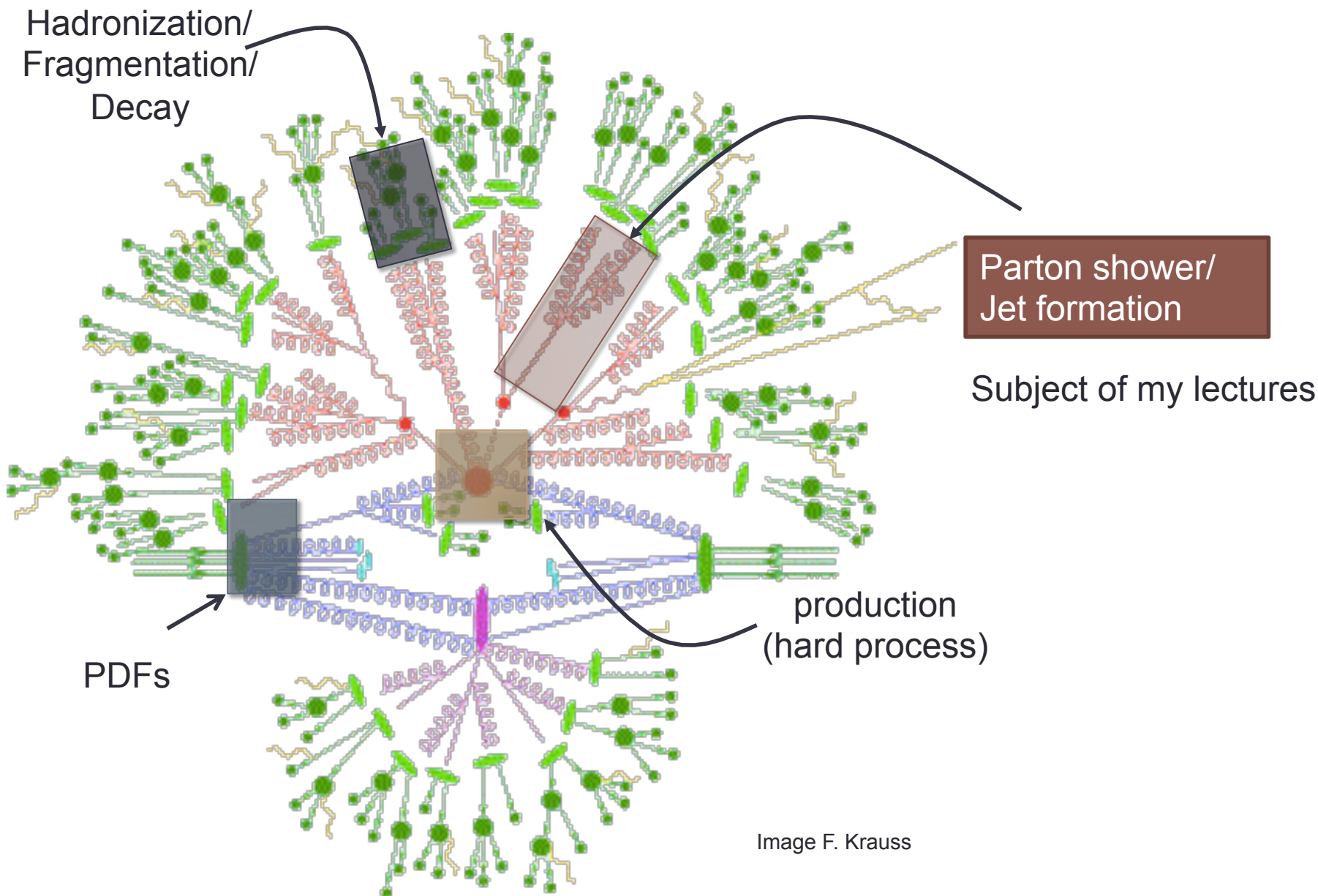
$$d\sigma = [\text{PDFs}] \times [\text{production}] \times [\text{parton shower}] \times [\text{hadronization}]$$

short distance
 long distance

Factorization

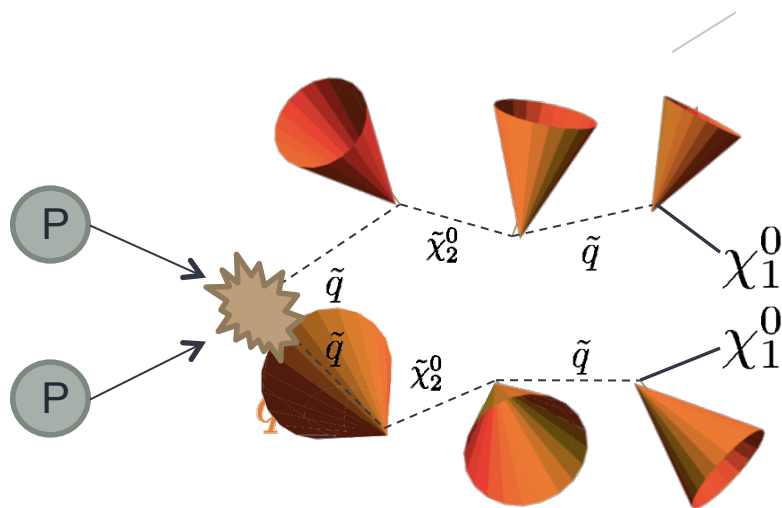
- Physics at different length scales can be calculated separately and then combined

$$d\sigma = [\text{PDFs}] \times [\text{production}] \times [\text{parton shower}] \times [\text{hadronization}]$$



Factorization

- Partons produced at short distances



6 Jets

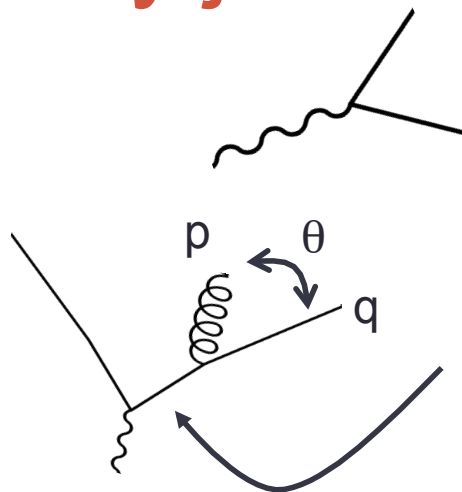
- Radiation and hadronization cannot change parton momentum by much

Short distance physics
imprinted on jets!

JETS FROM PERTURBATIVE QCD

Why jets?

Leading order: $R=0$, Energy = E



Propagator factor: $\frac{1}{(p+q)^2} = \frac{1}{2p \cdot q} = \frac{1}{E_p E_q (1 - \cos \theta)} = \frac{1}{2E_q E_p \sin^2 \frac{\theta}{2}}$

Blows up when $E=0$ (soft divergence)
Or $\theta = 0$ (collinear divergence)

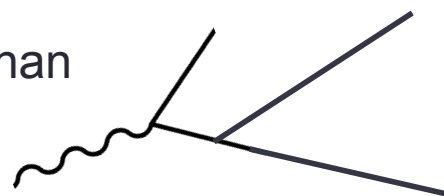
$$d\sigma \sim \alpha_s \int_0^R \frac{d\theta}{\theta} \frac{dE}{E} \sim \alpha_s \ln R \ln E$$

Sudakov double
logarithms

Rate for



much greater than



Collinear limit

In the **collinear** limit, cross sections factorize

$$\begin{array}{c} \text{Diagram 1} \end{array} + \begin{array}{c} \text{Diagram 2} \end{array} = \begin{array}{c} \text{Diagram 3} \end{array} \times \begin{array}{c} \text{Diagram 4} \end{array}$$

when $k_T^{(2)} \ll k_T^{(1)} \ll E_{\text{jet}}$

In the collinear limit, cross sections given by **DGLAP splitting functions**

$$\begin{array}{c} \text{Diagram 1} \end{array} = \begin{array}{c} \text{Diagram 2} \end{array} \times P_{q \rightarrow qg} \quad \frac{4}{3} \frac{\alpha}{2\pi} \frac{1+z^2}{1-z} \frac{1}{k_T^2}$$

$$\begin{array}{c} \text{Diagram 3} \end{array} = \begin{array}{c} \text{Diagram 4} \end{array} \times P_{g \rightarrow gg} \quad 3 \frac{\alpha}{2\pi} \left[\frac{z}{1-z} + \frac{1-z}{z} \right] \frac{1}{k_T^2}$$

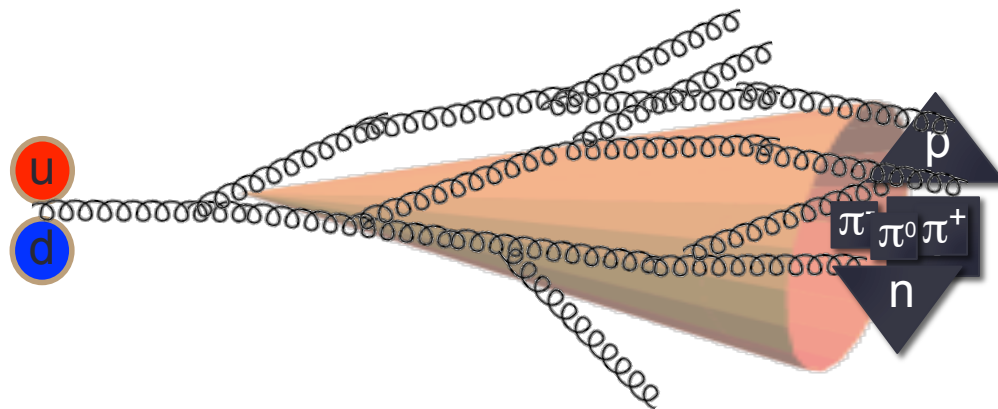
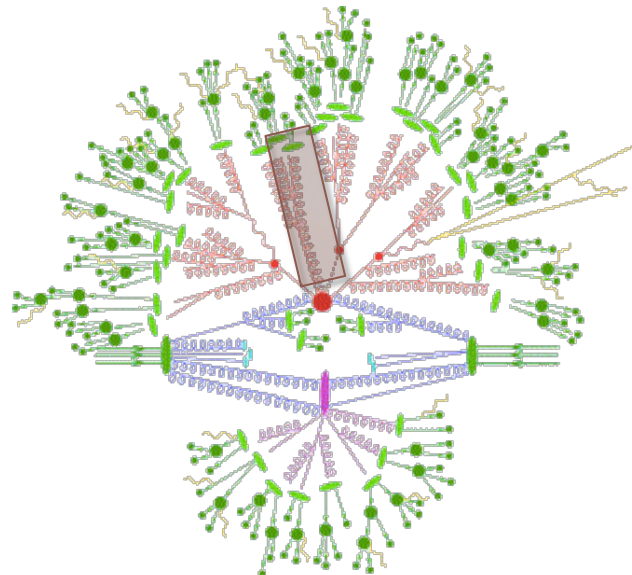
$z = \frac{E_1}{E_1 + E_2}$

Parton shower

Probability of finding a gluon with energy fraction z and transverse momentum k_T

$$dP = \frac{4}{3} \frac{\alpha}{2\pi} \frac{1+z^2}{1-z} \frac{1}{k_T^2} dk_T^2 dz$$

- Start with the largest scale ($k_T \sim Q$)
- Is there an emission?
- If not, try lower scales.



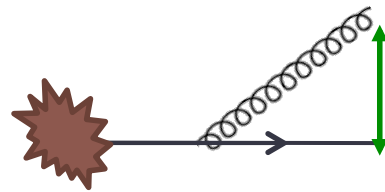
Parton “evolves” from hard scale to Λ_{QCD}

Sudakov factors

$$d\sigma = \frac{\alpha}{2\pi} \frac{1}{t} \frac{1+z^2}{1-z} dt dz$$

Integrate over z

$$d\sigma = P(t) dt = C_F \frac{\alpha_s}{2\pi} \frac{1}{t} \left(\ln \frac{t}{Q^2} + \frac{3}{2} \right)$$



$t \sim k_T^2 \sim \text{invariant mass}$

Probability of finding a gluon with energy fraction z and transverse momentum $t \sim k_T^2$

Probability of finding a gluon at this t

What is the scale for the hardest gluon?

- Should correspond to scale of the second hardest jet

Sudakov factor $\Delta(t_0, t)$ is the probability of finding no gluons between t_0 at t

$$\Delta(t_0, t + \delta t) = \Delta(t_0, t) \left(1 - \int_t^{t+\delta t} dt' P(t') \right) = \Delta(t_0, t) - P(t) \delta t \Delta(t_0, t)$$

$$\Delta(t_0, t + \delta t) = \Delta(t_0, t) + \delta t \frac{d}{dt} \Delta(t_0, t)$$

$$\left. \begin{array}{l} \Delta(t_0, t + \delta t) = \Delta(t_0, t) \left(1 - \int_t^{t+\delta t} dt' P(t') \right) \\ \Delta(t_0, t + \delta t) = \Delta(t_0, t) + \delta t \frac{d}{dt} \Delta(t_0, t) \end{array} \right\} \frac{d}{dt} \Delta(t_0, t) = -P(t) \Delta(t_0, t)$$

$$\text{Thus, } \Delta(t_0, t) = \exp \left(- \int_{t_0}^t P(t') dt' \right) \sim \exp \left[- \frac{2\alpha_s}{3\pi} \left(\ln^2 \frac{t}{Q} + \frac{3}{2} \ln \frac{t}{Q} \right) \right]$$

And so, the cross section for the hardest gluon is

$$d\sigma = \Delta(Q, t) P(t) dt \approx e^{-\frac{2\alpha_s}{3\pi} \ln^2 \frac{t}{Q}} \frac{dt}{t}$$

Sudakov factor
= semi-classical resummation
of the leading Sudakov logarithm

Parton shower

- Probability of emission at some t

$$d\sigma = P(t)dt = C_F \frac{\alpha_s}{2\pi} \frac{1}{t} \left(\ln \frac{t}{Q^2} + \frac{3}{2} \right)$$

- Probability that hardest emission is at t

$$d\sigma = \Delta(Q, t) P(t) dt \approx \underbrace{e^{-\frac{2\alpha_s}{3\pi} \ln^2 \frac{t}{Q^2}}}_{\text{Leading log resummation}} \frac{dt}{t}$$

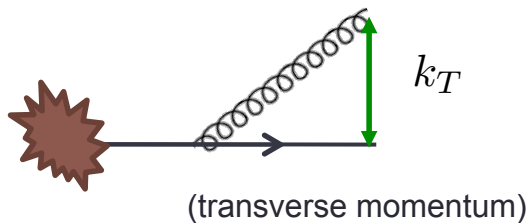
Leading log resummation

- Agrees with cross section for hardest parton in QCD including leading log resummation

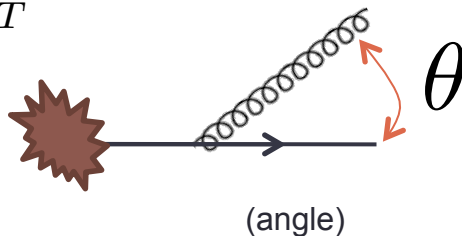
$$k_T^2 = tz(1-z) \Rightarrow \frac{dk_T^2}{k_T^2} = \frac{dt}{t}$$

- Formally correct at this order for many **scale choices**

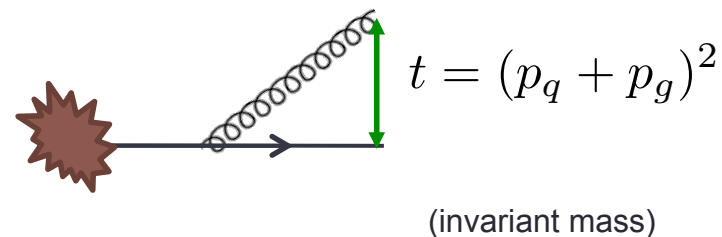
$$d\sigma \approx e^{-\frac{2\alpha_s}{3\pi} \ln^2 \frac{k_T^2}{Q^2}} \frac{dk_T^2}{k_T^2}$$



$$d\sigma \approx e^{-\frac{2\alpha_s}{3\pi} \ln^2 \theta} \frac{d\theta}{\theta}$$



$$d\sigma \approx e^{-\frac{2\alpha_s}{3\pi} \ln^2 \frac{t}{Q^2}} \frac{dt}{t}$$



- Common scale choices **motivated** by **soft physics**

Parton shower

- Semi-classical model which agrees with perturbative QCD in **collinear limit** at **leading-logarithmic** level

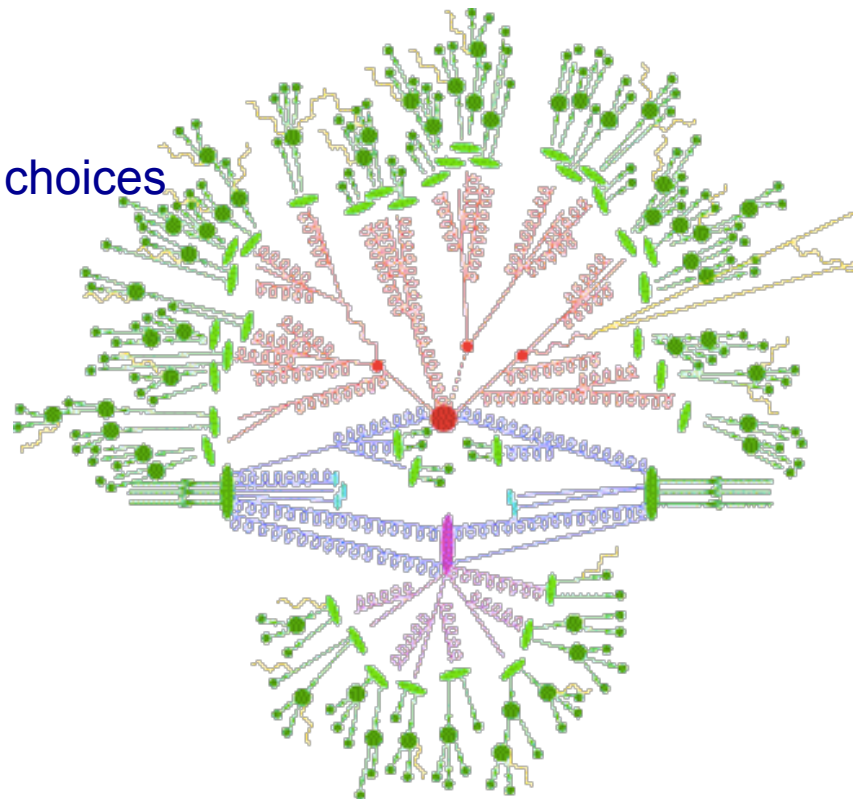
$$d\sigma = e^{-\int dP} dP$$

$$\sim \underbrace{e^{-\alpha \ln^2\left(\frac{\mu_1}{\mu_2}\right)}}_{\text{Leading log resummation}} \left(\frac{\alpha_s}{2\pi} \frac{1+z}{1-z^2} \right) dz$$

DGLAP
splitting functions

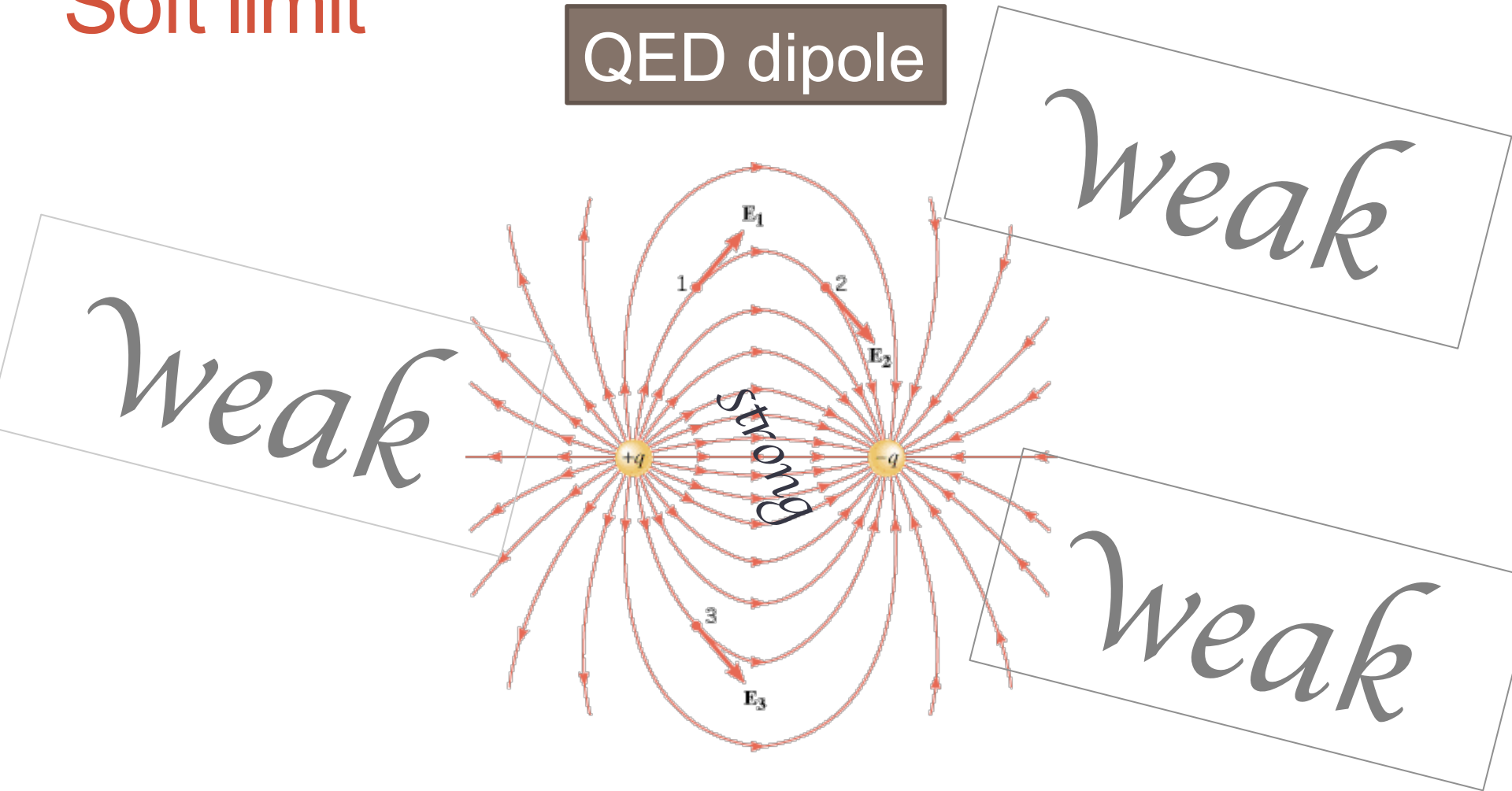
Leading log resummation

- Formally correct at this order for many **scale choices**
- Common scale choices **motivated** by **soft physics**



Soft limit

QED dipole

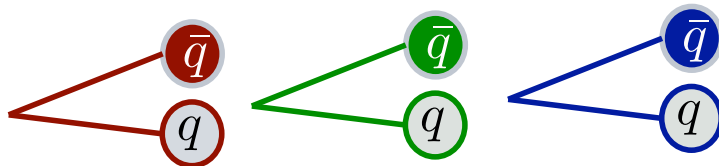


- In soft limit (large distance limit), field from $+$ and $-$ charges cancel
- Coherent destructive **interference**

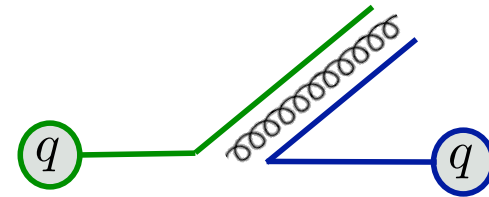
Soft limit

QCD

3 quark color dipoles

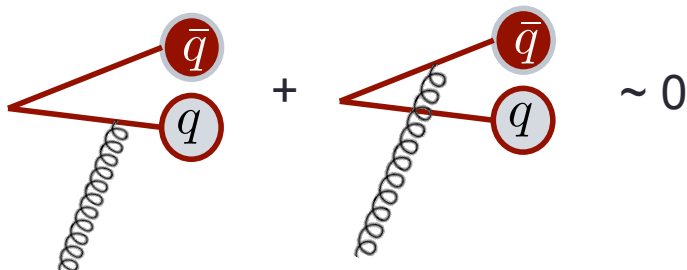


Gluons act like ends of 2 dipoles



Accurate up to $1/N^2 \sim 10\%$ effects

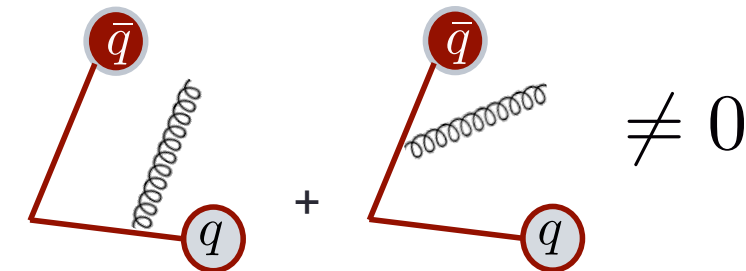
Destructive interference



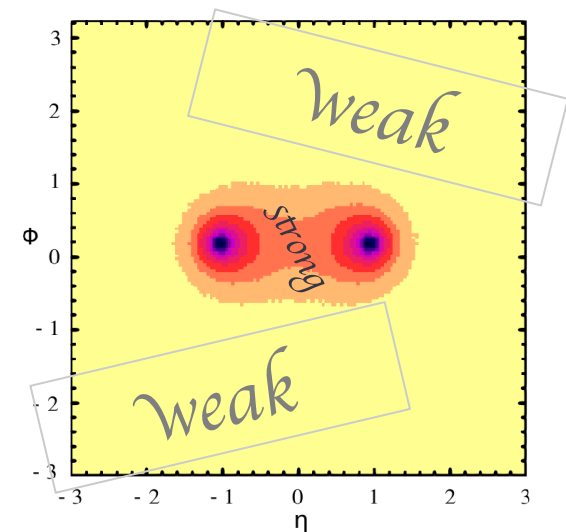
Color coherence



Angular ordering



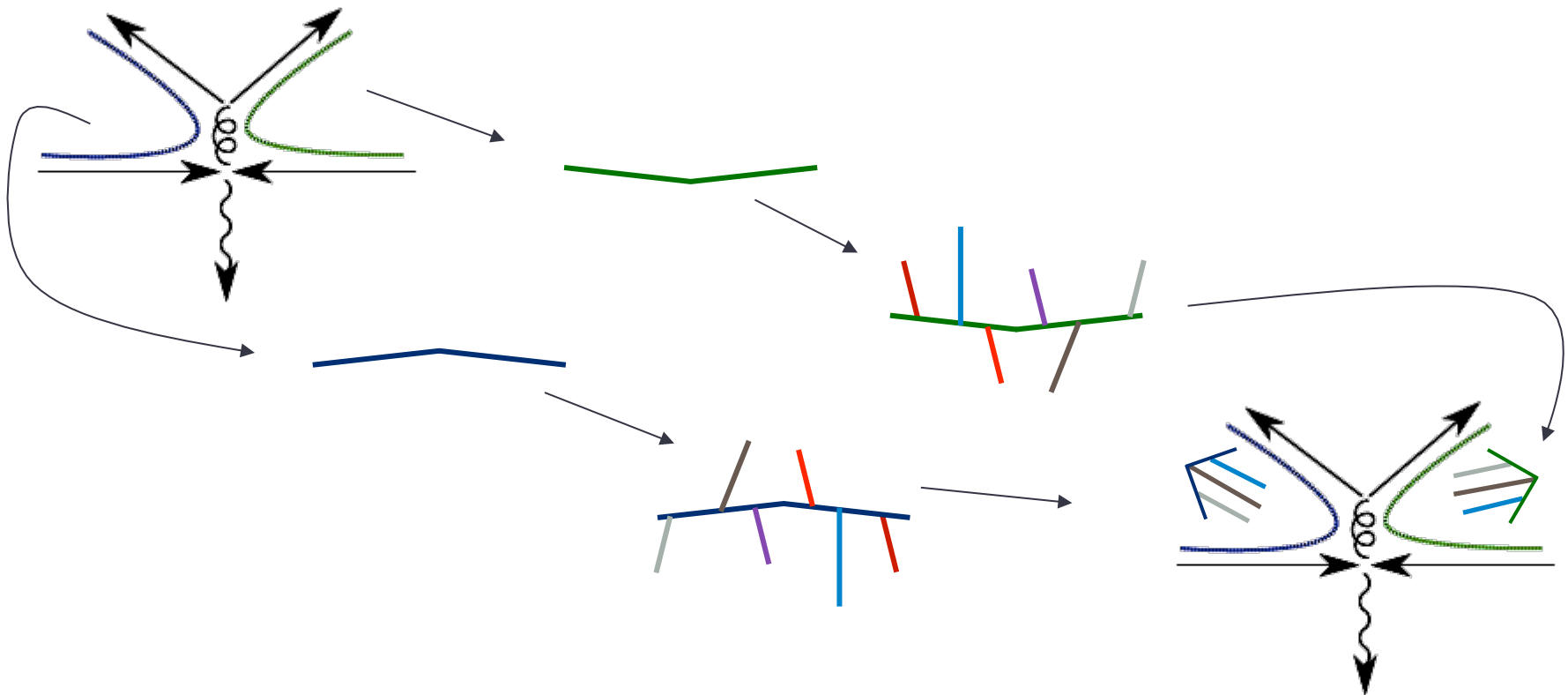
Constructive interference



Pythia simulation

Dipole shower

Dipole showers in its rest frame



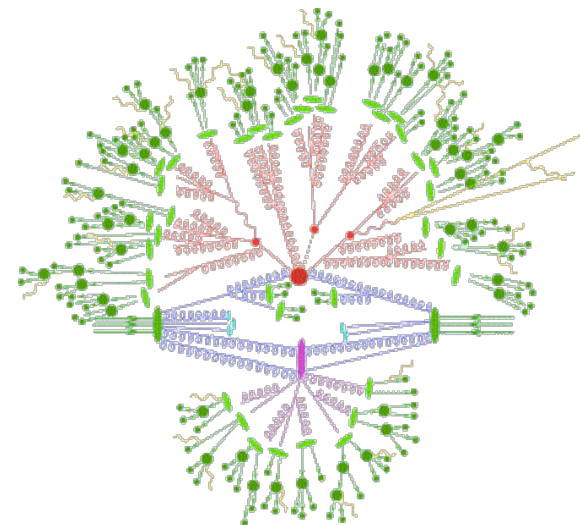
- Boost \rightarrow **string showers** in **dipole-momentum** direction
- Alternative to angular ordering

Parton shower summary

- Semi-classical model which agrees with perturbative QCD in **collinear limit** at **leading-logarithmic** level

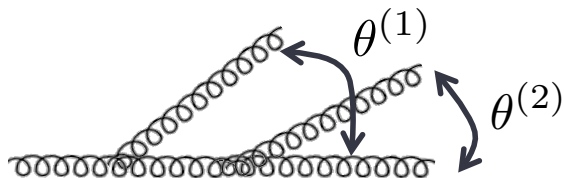
$$d\sigma \approx e^{-\int dP dP} \approx e^{-\frac{2\alpha_s}{3\pi} \ln^2 \frac{\mu^2}{Q^2}} \frac{d\mu}{\mu}$$

Suadkov factor
(leading log resummation)

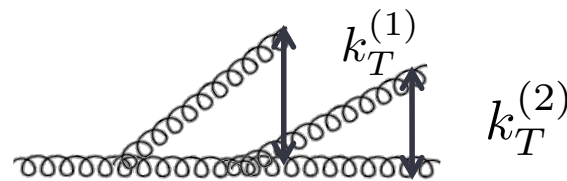


- Formally correct at **leading log** in the **collinear limit**

Herwig uses an angle ordered shower



Pythia uses a k_T ordered dipole shower



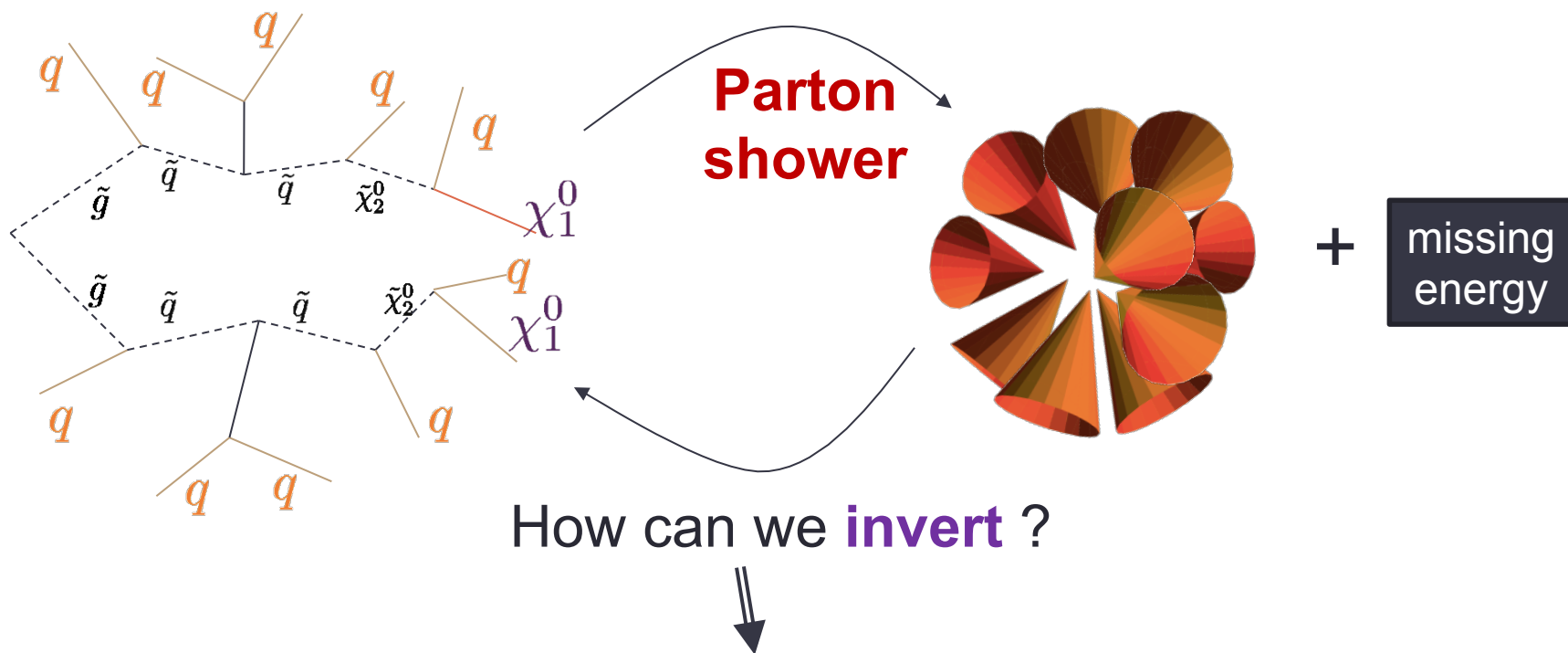
- Both incorporate **color coherence**
- Neither gets soft limit exactly right
- Parton showers give **amazingly accurate** simulations of complicated final states

JET ALGORITHMS

Jet-parton-map

We want to see quarks and gluons:

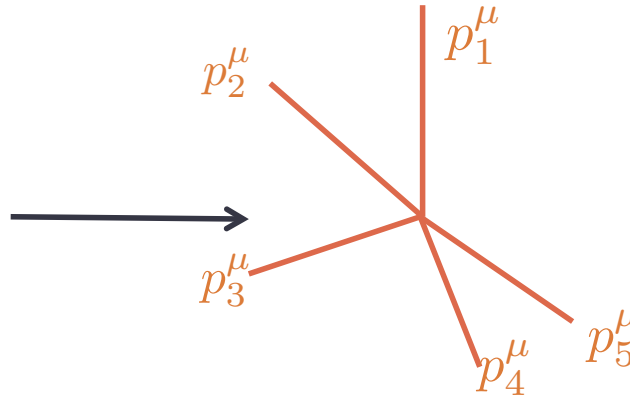
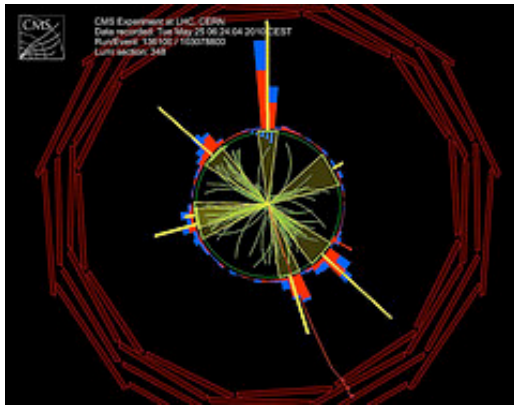
We observe jets:



- Find jet momenta
- Set quark momenta = jet momenta

Jet algorithms

- Construct jet 4-momentum from observed particle 4-momenta



Desirable properties

- Good match between jet and parton momenta
- Insensitive to hadronization
- Calculable in perturbative QCD = infrared safe
- Experiment friendly
 - Easy to calibrate
 - Insensitive to pileup
- Fast

Cone algorithms

- Conceptually simple
- Difficulties with infrared safety

Iterative algorithms

- Popular
- Efficient

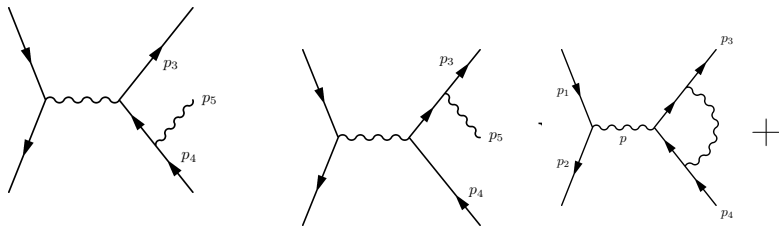
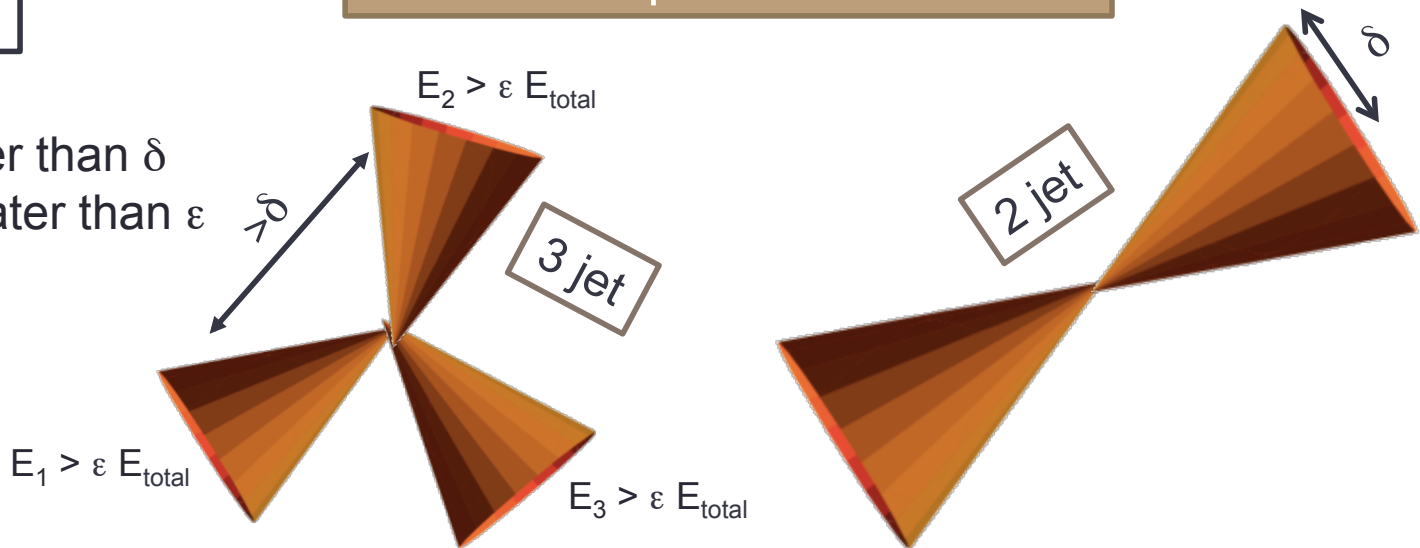
Sterman-Weinberg jets (1977)

e^+e^- to 2 or 3 jets

Jets from perturbative QCD

3 jets if:

- **Angles** greater than δ
- **Energies** greater than ϵ



Would blow up if
We just asked for cones
(no energy restriction)

$$\sigma_{2\text{jet}} = \sigma_0 \left[1 - \frac{\alpha_s}{2\pi} \left(\ln \delta \ln \epsilon + \ln \delta - \frac{3}{4} + \dots \right) \right]$$

- This jet definition is **infrared safe** (finite in perturbation theory)

Cone jets

Generalizations to hadron colliders

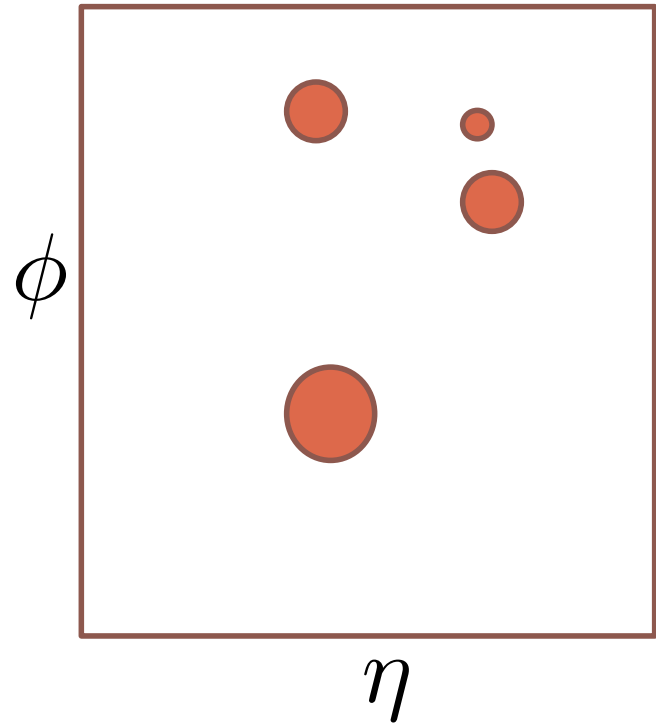
- Where are the cones centered
 - Seeded cones, Fixed cones, Midpoints
- Is it still infrared safe
 - Maybe, maybe not. Does it matter?

Processing Finding cones	Progressive Removal	Split–Merge	Split–Drop
Seeded, Fixed (FC)	GetJet CellJet		
Seeded, Iterative (IC)	CMS Cone	JetClu (CDF) [†] ATLAS cone	
Seeded, It. + Midpoints (IC _{mp})		CDF MidPoint D0 Run II cone	PxCone
Seedless (SC)		SISCone	

Iterative jet algorithms

- Start with input **4-vectors**
 - e.g. stable particles, topoclusters, calorimeter cells, etc.
- **Calculate** the pairwise distances

$$R_{ij} = \sqrt{(\theta_i - \theta_j)^2 + (\eta_i - \eta_j)^2}$$



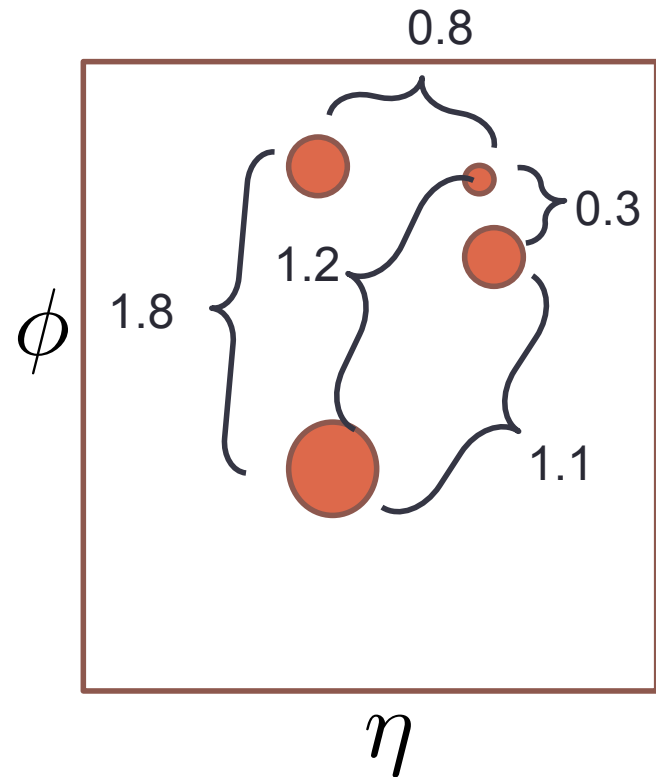
Iterative jet algorithms

- Start with input **4-vectors**
 - e.g. stable particles, topoclusters, calorimeter cells, etc.

- **Calculate** the pairwise distances

$$R_{ij} = \sqrt{(\theta_i - \theta_j)^2 + (\eta_i - \eta_j)^2}$$

- **Merge** the two closest particles



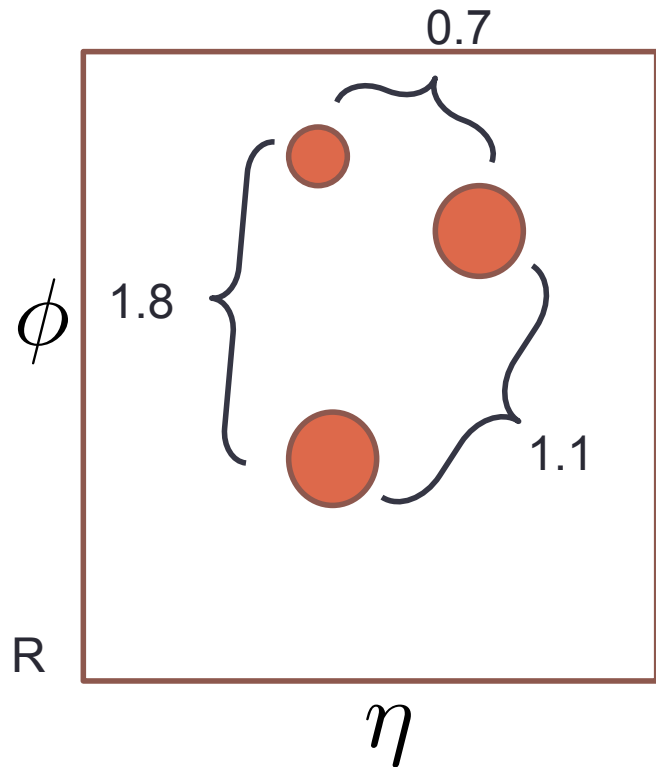
Iterative jet algorithms

- Start with input **4-vectors**
 - e.g. stable particles, topoclusters, calorimeter cells, etc.

- **Calculate** the pairwise distances

$$R_{ij} = \sqrt{(\theta_i - \theta_j)^2 + (\eta_i - \eta_j)^2}$$

- **Merge** the two closest particles
- **Repeat** until no two particles are closer than R



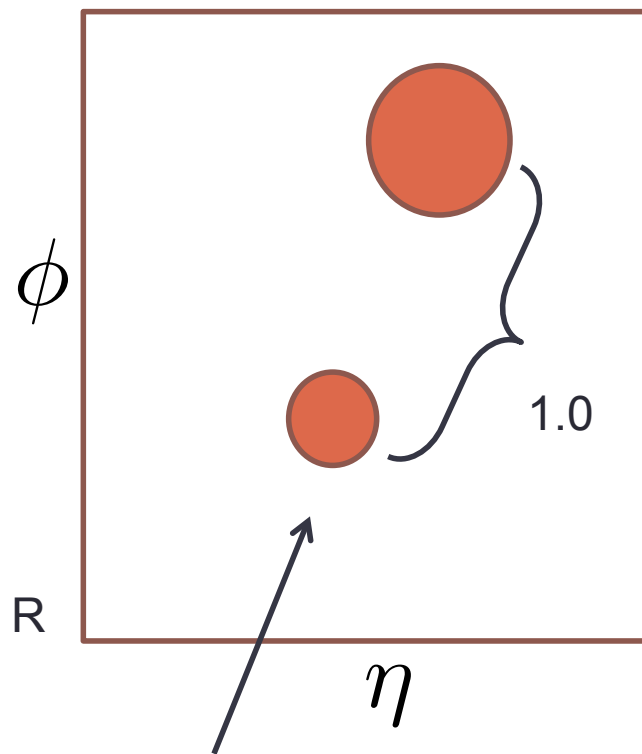
Iterative jet algorithms

- Start with input **4-vectors**
 - e.g. stable particles, topoclusters, calorimeter cells, etc.

- **Calculate** the pairwise distance

$$R_{ij} = \sqrt{(\theta_i - \theta_j)^2 + (\eta_i - \eta_j)^2}$$

- **Merge** the two closest particles
- **Repeat** until no two particles are closer than R

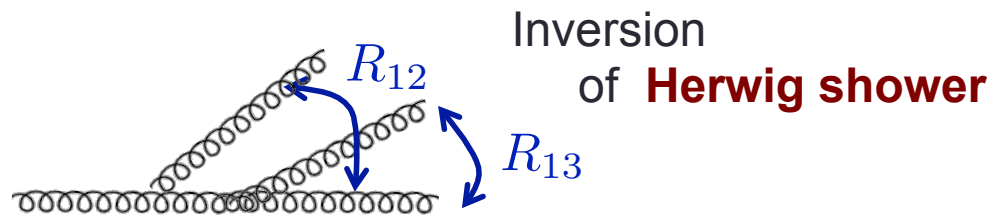


Different distance measures

Cambridge/Aachen algorithm

$$d_{ij} = \left(\frac{R_{ij}}{R_0} \right)^2$$

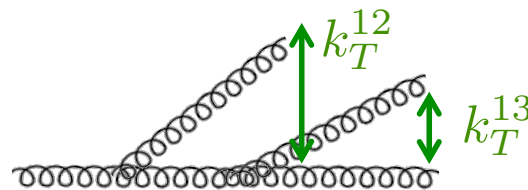
- clusters **closest** radiation **first**



k_T algorithm

$$d_{ij} = \min(p_{Ti}^2, p_{Tj}^2) \left(\frac{R_{ij}}{R_0} \right)^2$$

- clusters **hard collinear** radiation **first**



anti k_T algorithm

$$d_{ij} = \min(p_{Ti}^{-2}, p_{Tj}^{-2}) \left(\frac{R_{ij}}{R_0} \right)^2$$

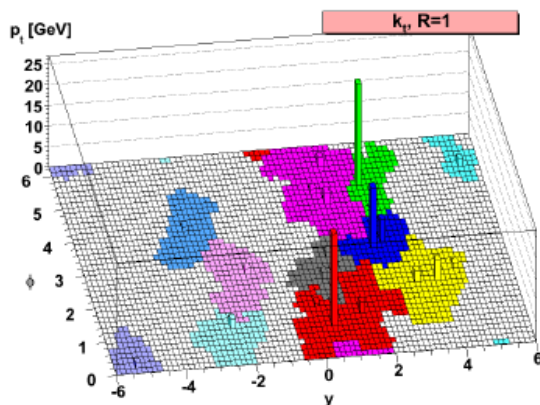
- Clusters farthest first
- No inverse parton-shower interpretation
- Produces round jets
- Almost exclusively used by ATLAS and CMS

Jet algorithms

Cacciari, Salam, Soyez JHEP 0804:063 (2008)

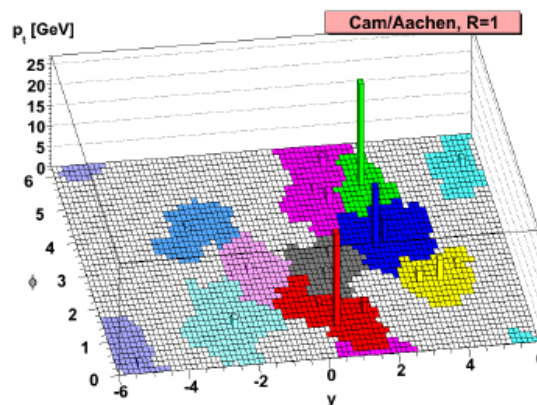
- popular at Tevatron
- Good for QCD theory
- Non-compact regions – hard to calibrate

k_T

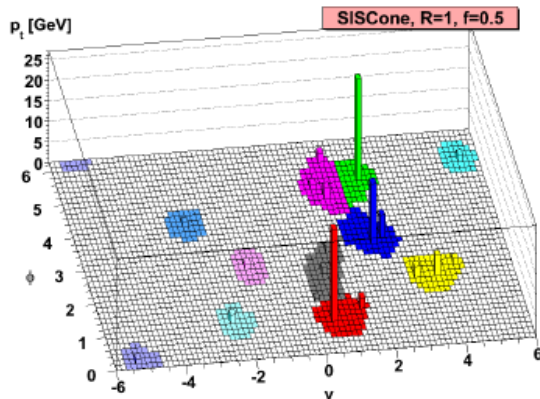


Cambridge/Aachen

- Based on angles
- Closer to cones



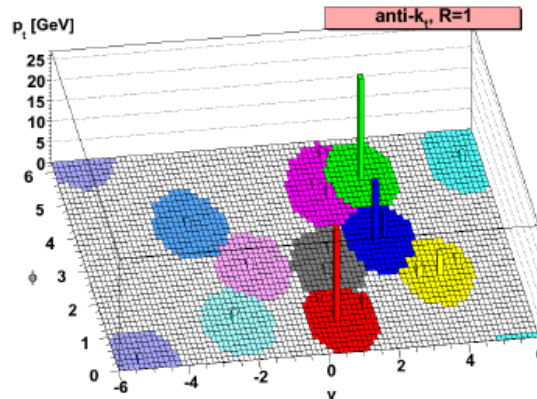
SISCone, R=1, f=0.5



SISCone

- Infrared safe cone algorithm
- Not cones at all

anti- k_T , R=1



Anti k_T

- Very round jets
- No parton shower interpretation
- Great for calibration

What R is best?

Goal: reconstruct parton momentum in Monte Carlo

- Include all final state radiation (FSR)

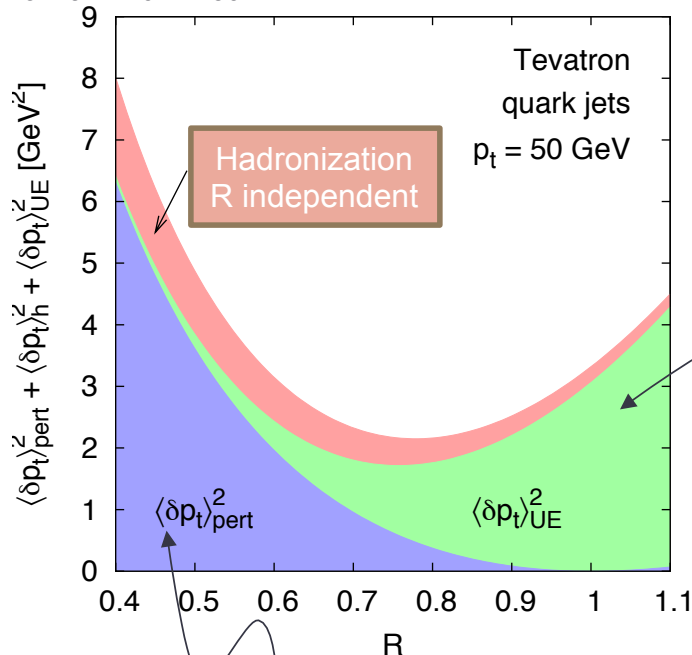
Bigger R

- Include little initial state radiation
- Include little pileup

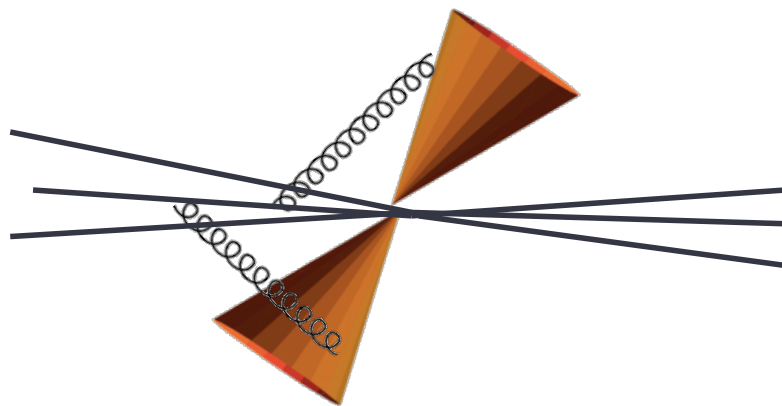
Smaller R

Jet p_T versus parton p_T

From arXiv:0712.3014



Underlying event (ISR, proton remnants)



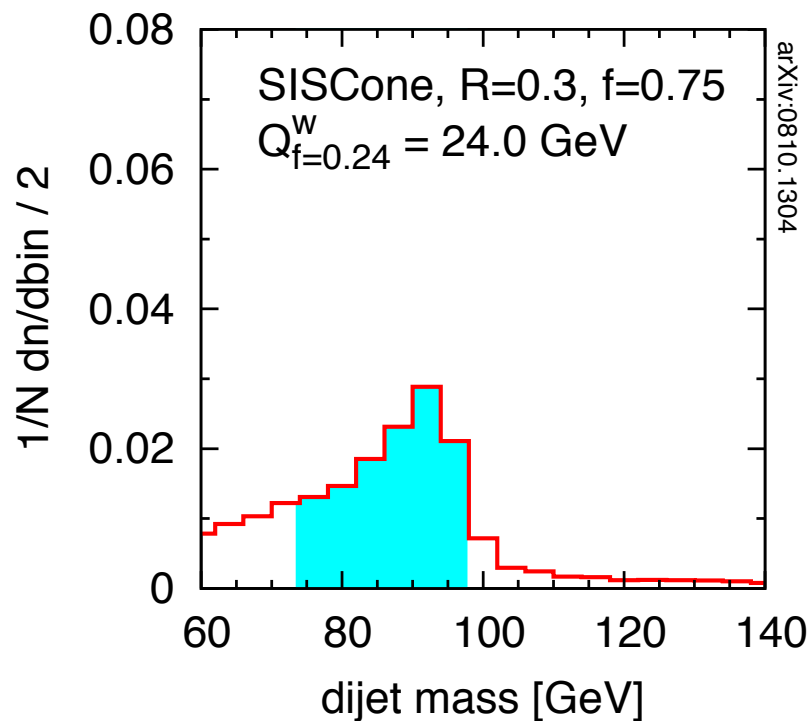
In practice

- $R \sim 0.4-0.7$ works best
- Must optimize for each study

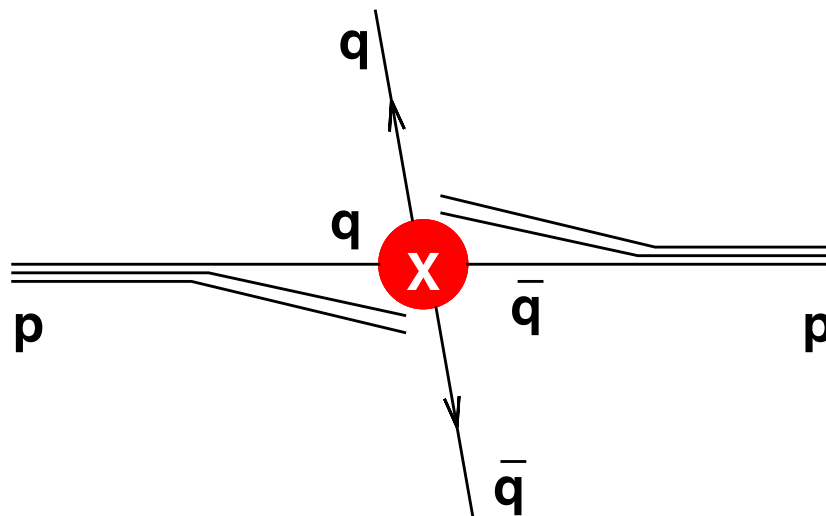
Resonance peak various R

$R = 0.3$

$qq, M = 100 \text{ GeV}$



Resonance X \rightarrow dijets



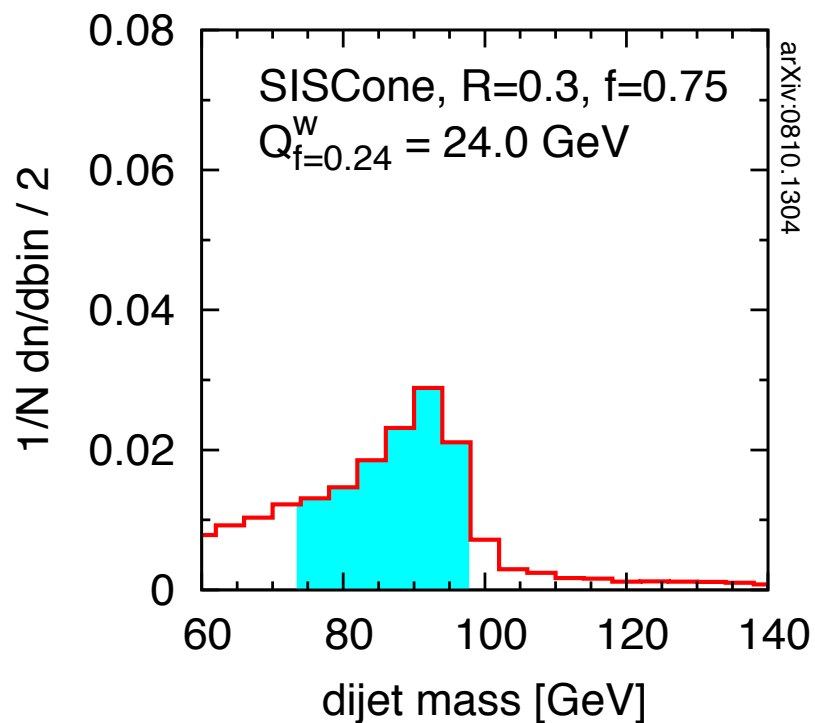
from G. Salam

<http://www.lpthe.jussieu.fr/~salam/jet-quality/>

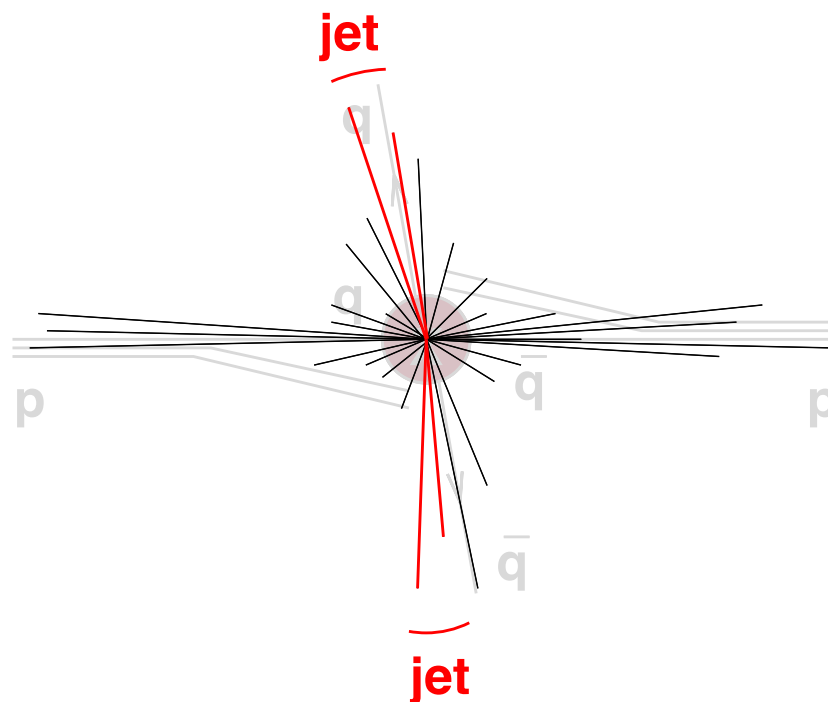
Resonance peak various R

R = 0.3

qq, M = 100 GeV



Resonance X \rightarrow dijets



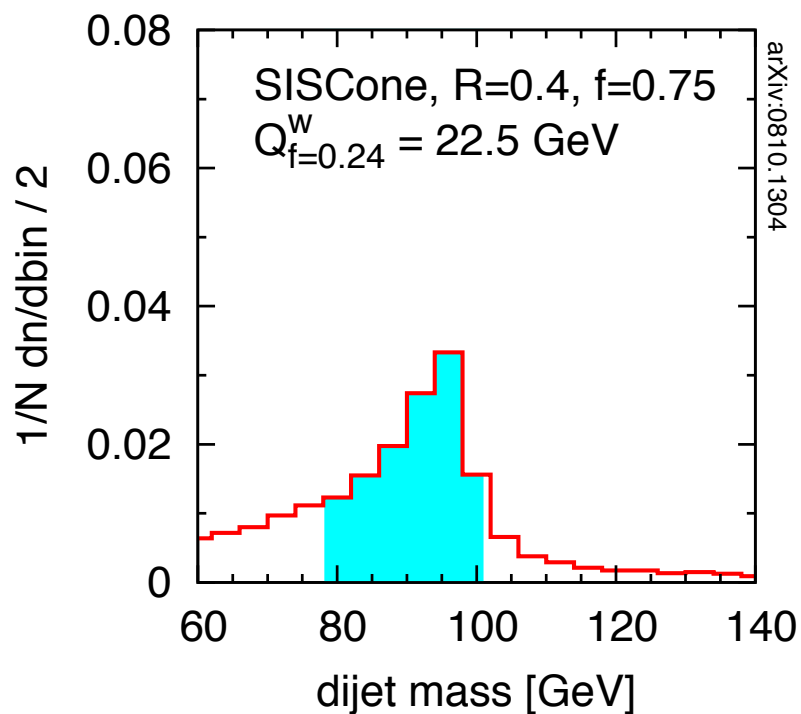
from G. Salam

<http://www.lpthe.jussieu.fr/~salam/jet-quality/>

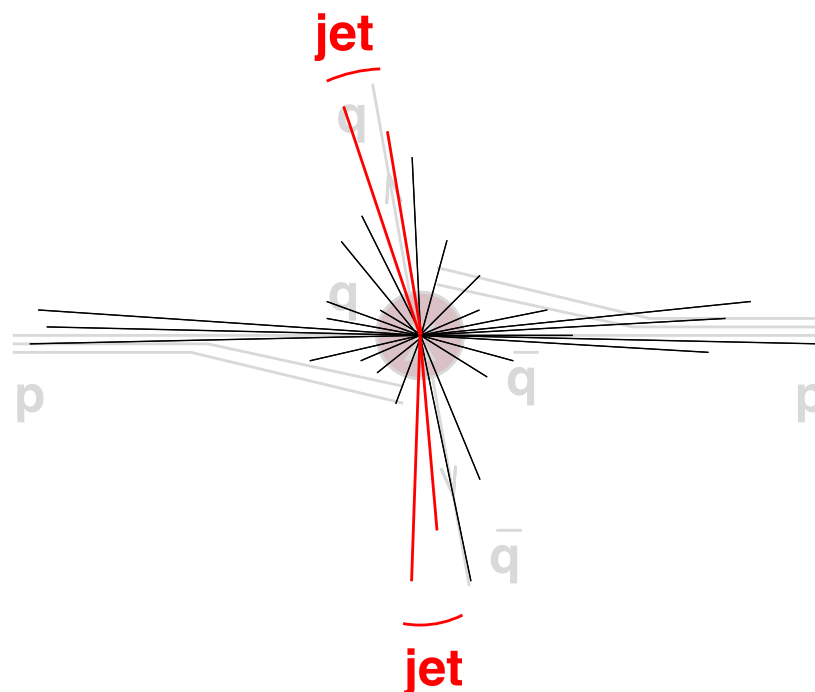
Resonance peak various R

$R = 0.4$

qq , $M = 100$ GeV



Resonance $X \rightarrow$ dijets



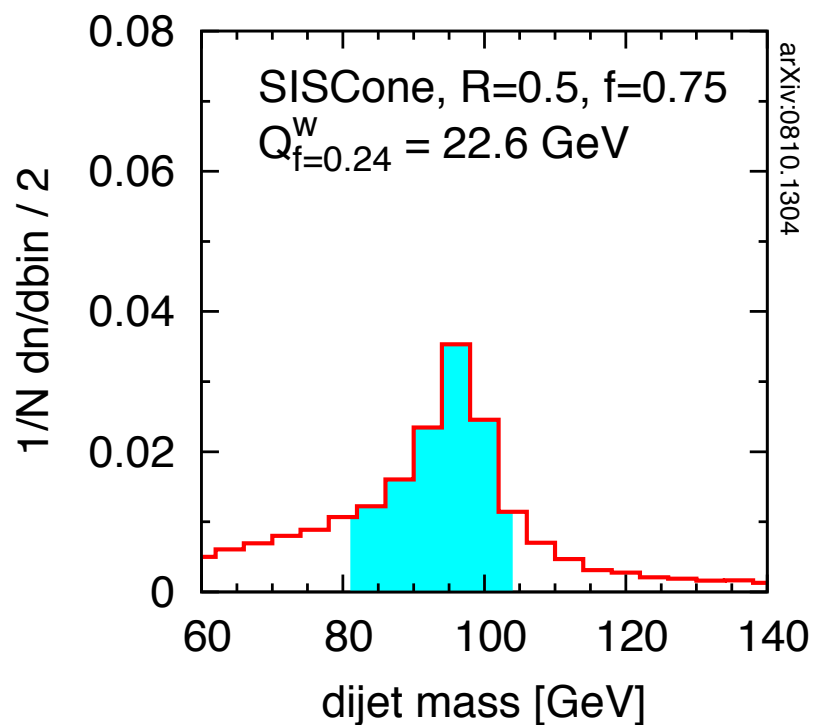
from G. Salam

<http://www.lpthe.jussieu.fr/~salam/jet-quality/>

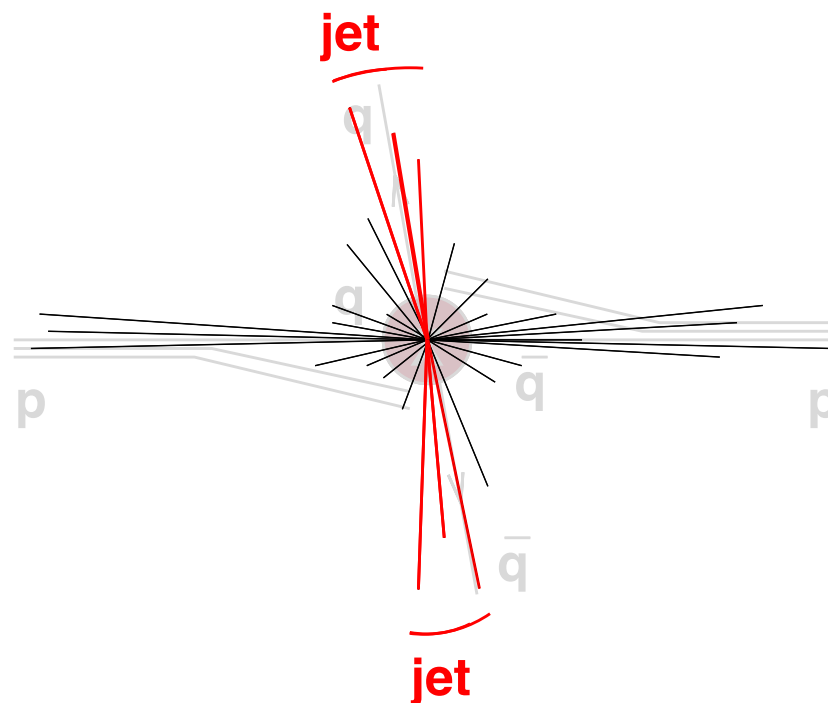
Resonance peak various R

R = 0.5

qq, M = 100 GeV



Resonance X \rightarrow dijets

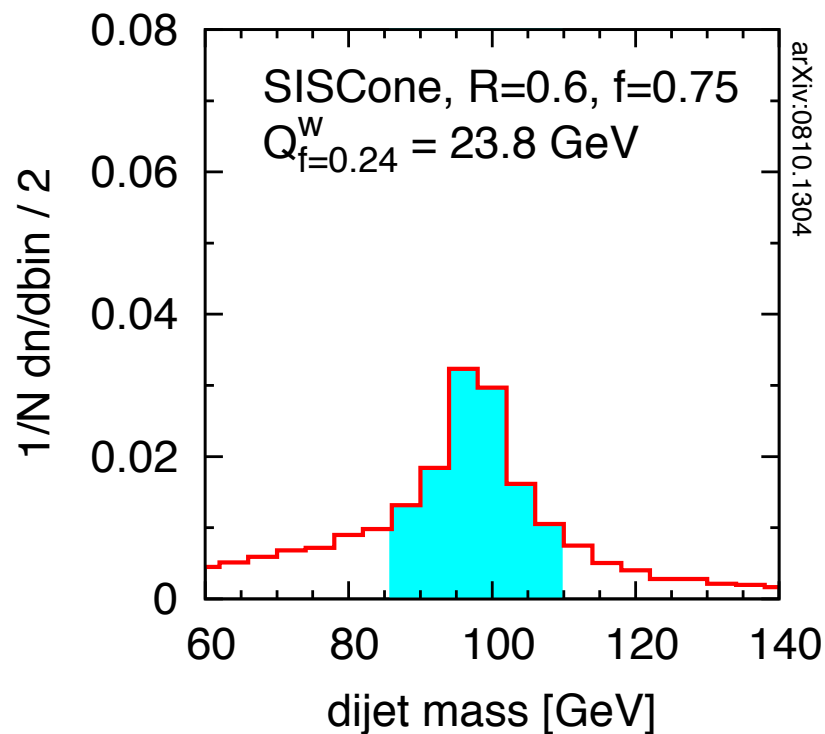


from G. Salam
<http://www.lpthe.jussieu.fr/~salam/jet-quality/>

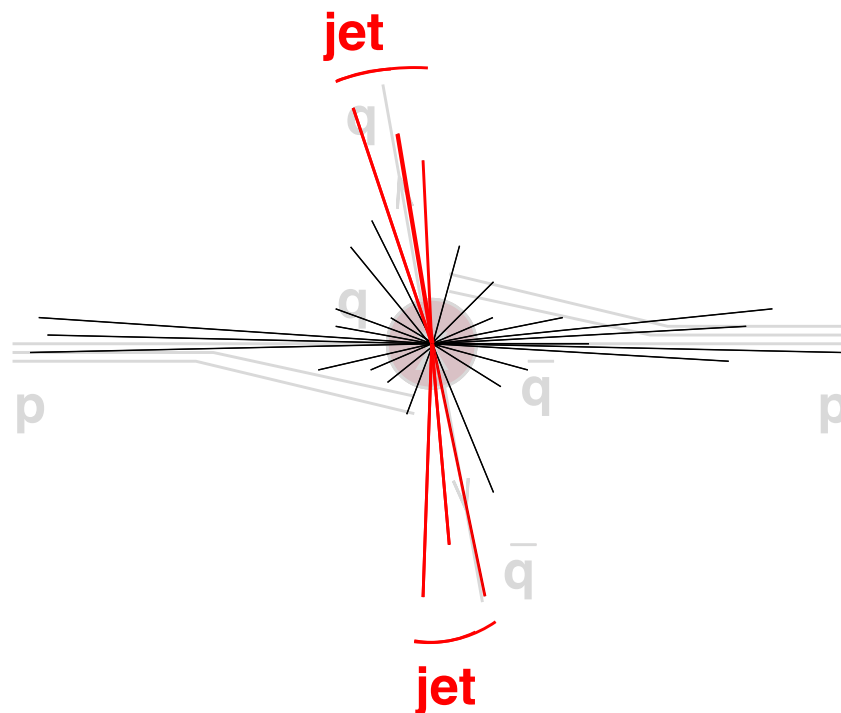
Resonance peak various R

R = 0.6

qq, M = 100 GeV



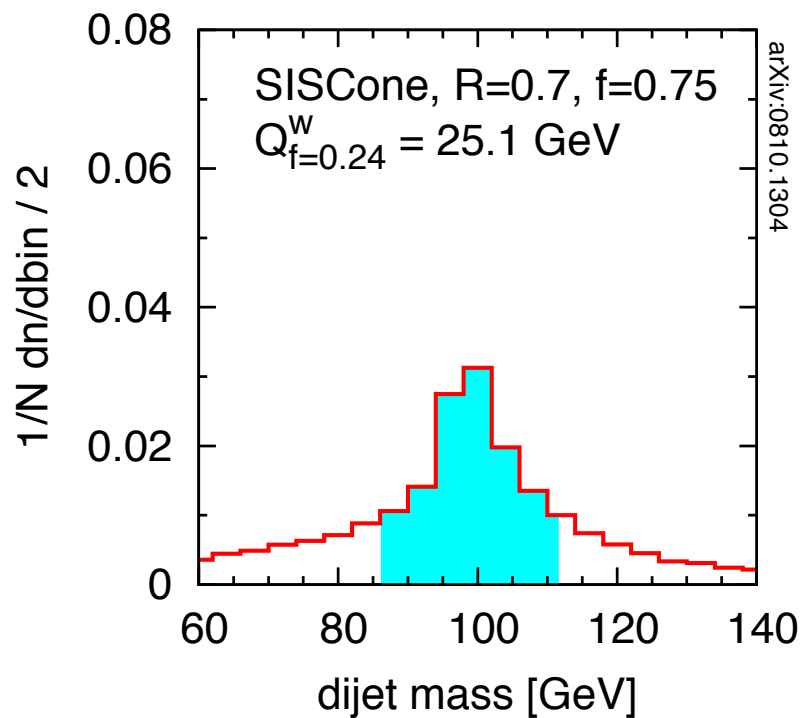
Resonance X \rightarrow dijets



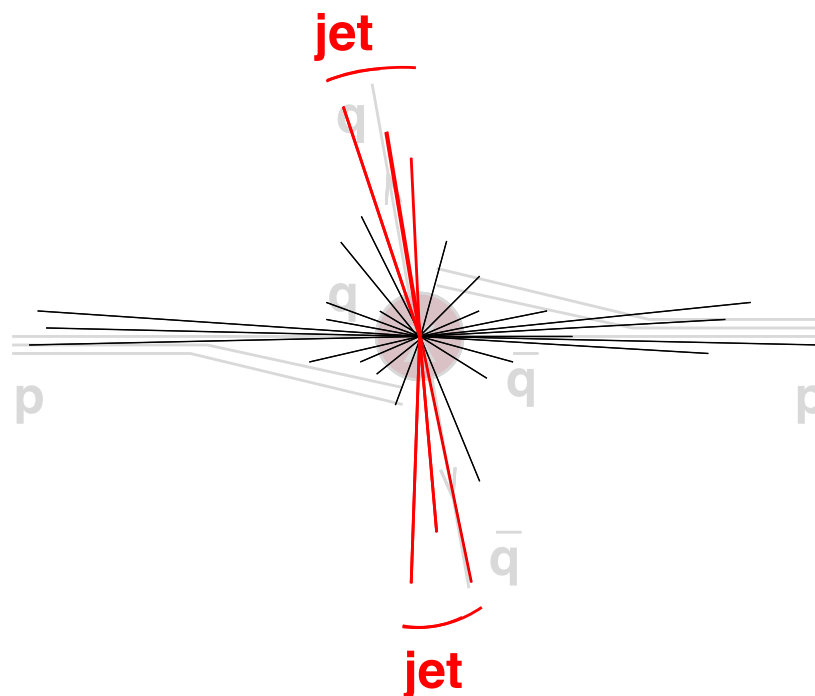
Resonance peak various R

R = 0.7

qq, M = 100 GeV



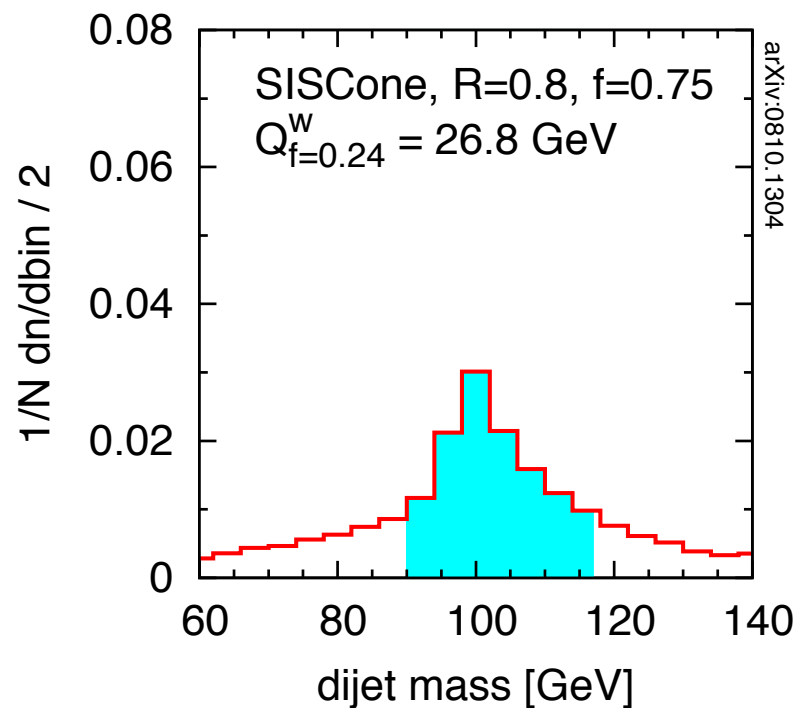
Resonance X \rightarrow dijets



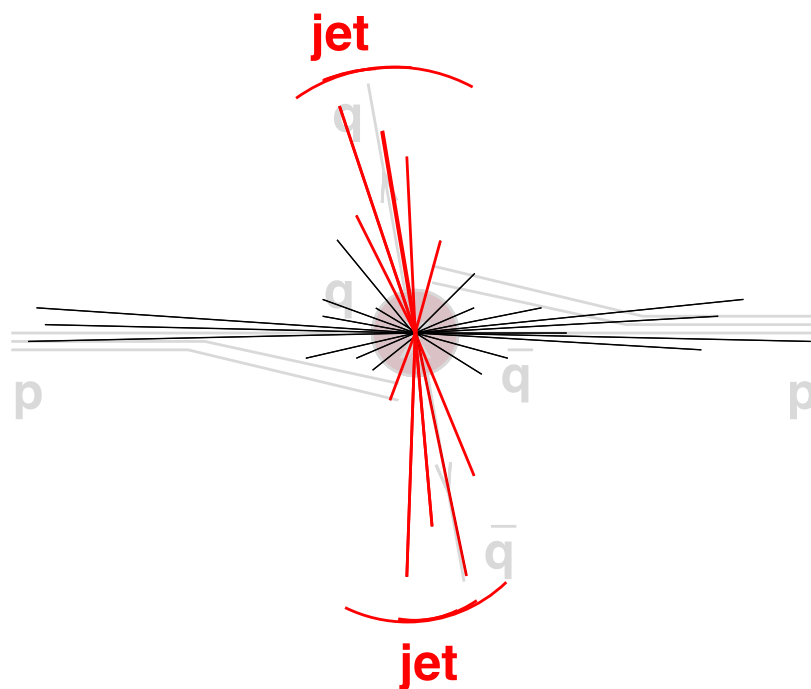
Resonance peak various R

$R = 0.8$

qq, $M = 100$ GeV



Resonance $X \rightarrow$ dijets



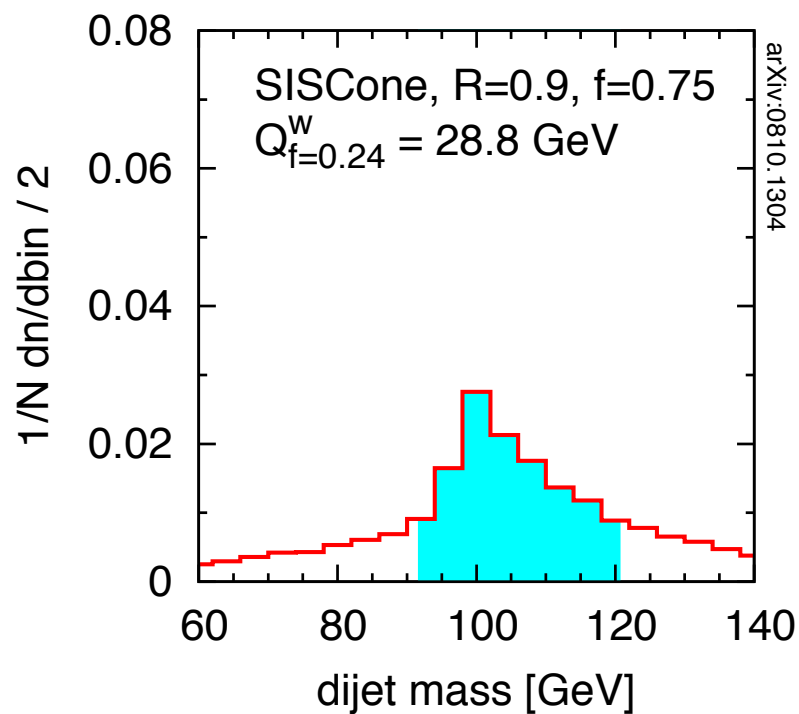
from G. Salam

<http://www.lpthe.jussieu.fr/~salam/jet-quality/>

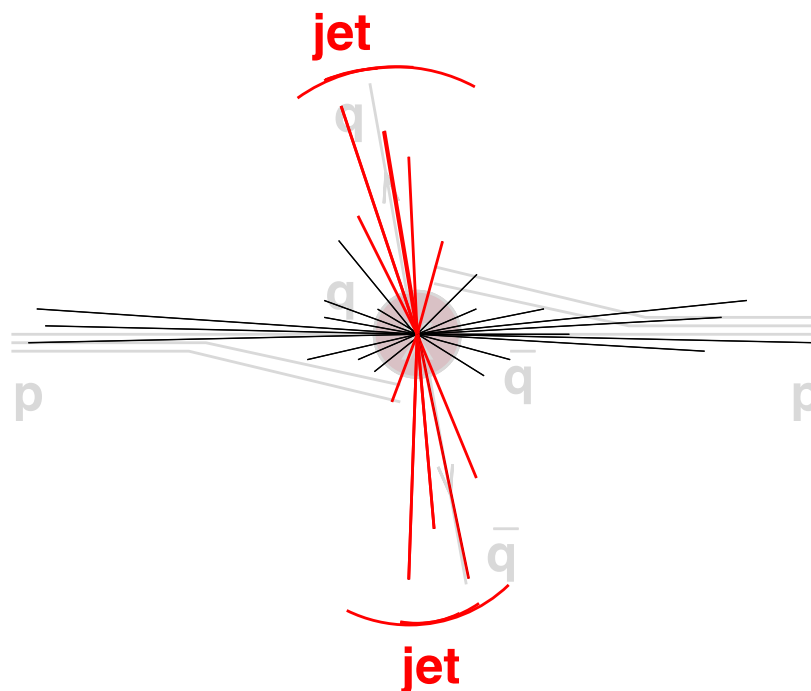
Resonance peak various R

$R = 0.9$

$qq, M = 100 \text{ GeV}$



Resonance $X \rightarrow$ dijets



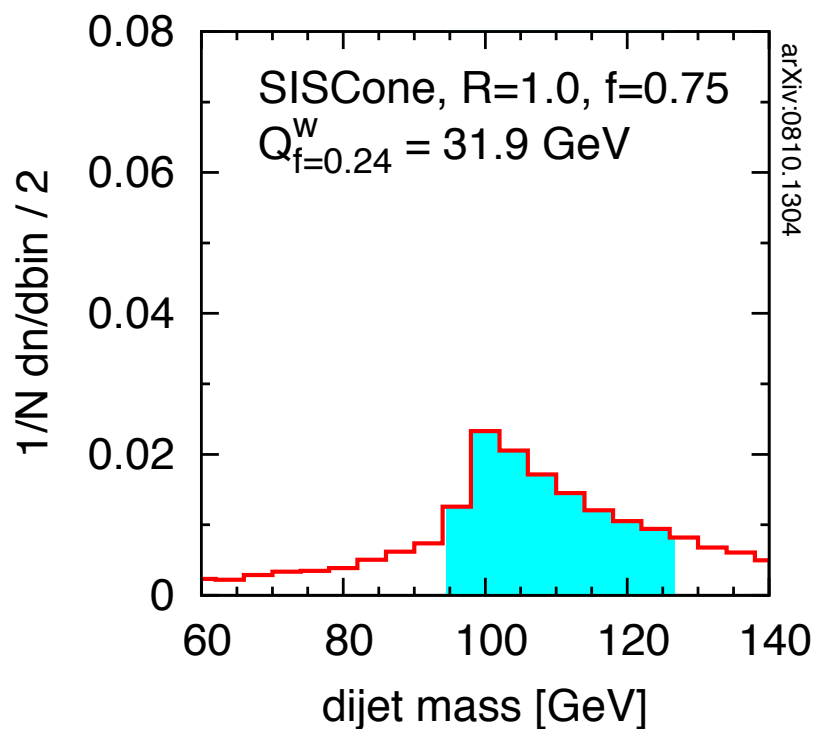
from G. Salam

<http://www.lpthe.jussieu.fr/~salam/jet-quality/>

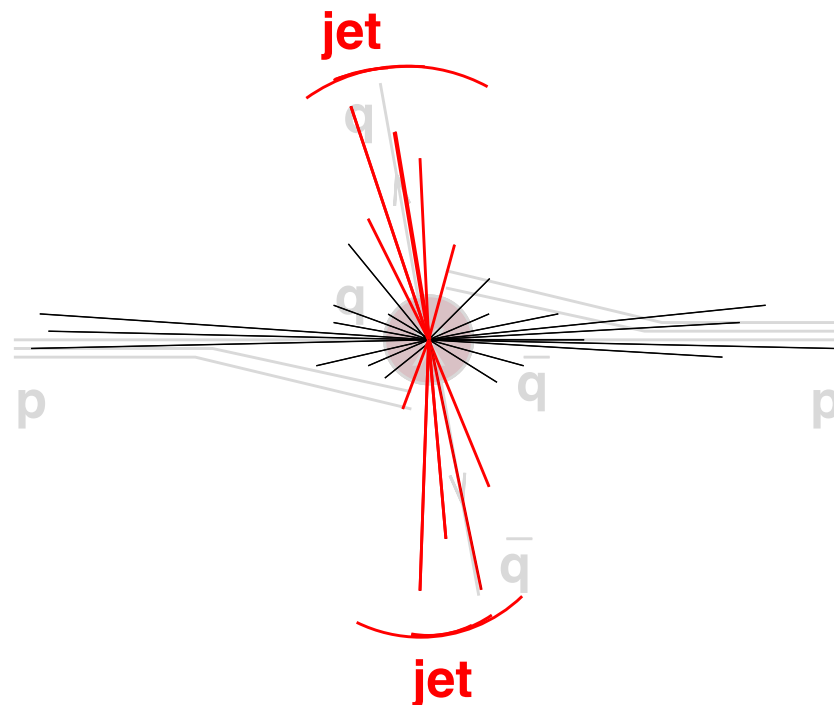
Resonance peak various R

R = 1.0

qq, M = 100 GeV



Resonance X \rightarrow dijets

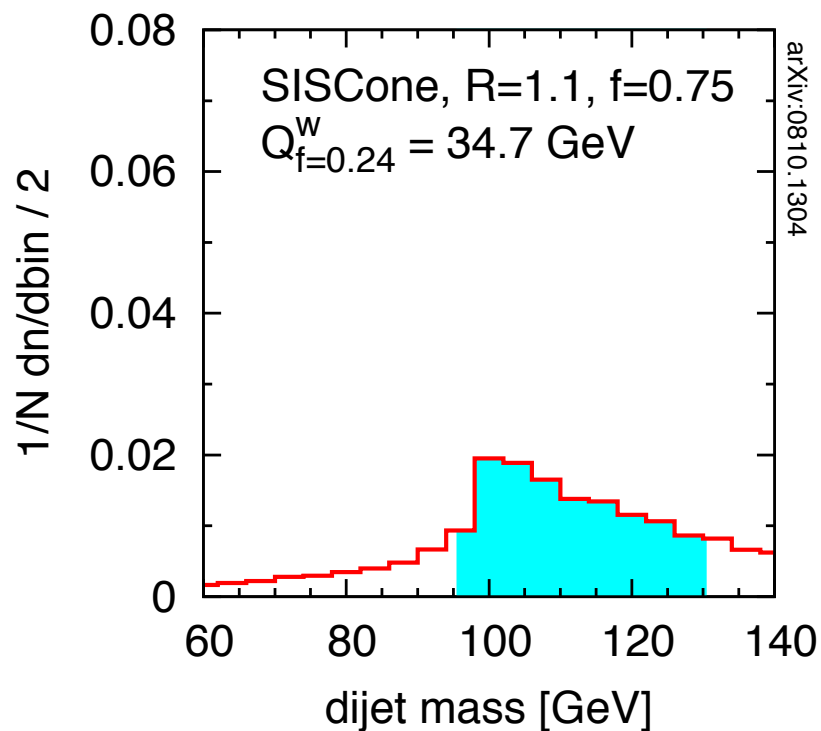


from G. Salam
<http://www.lpthe.jussieu.fr/~salam/jet-quality/>

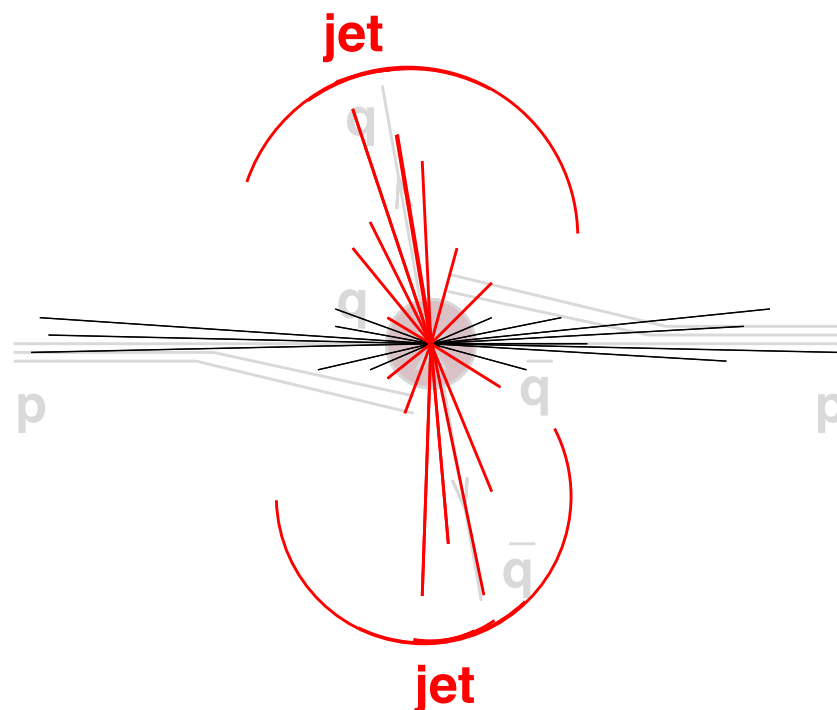
Resonance peak various R

R = 1.1

qq, M = 100 GeV



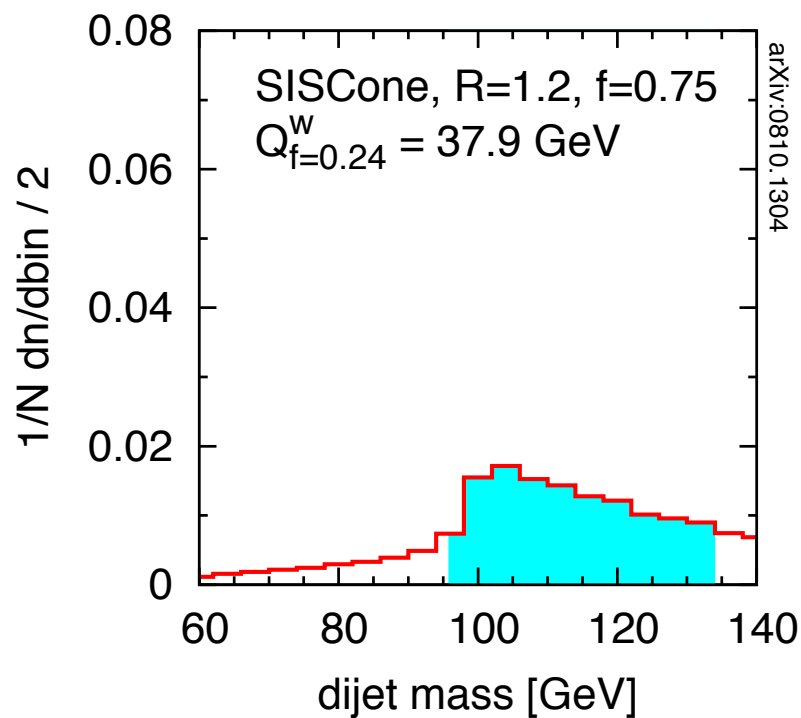
Resonance X \rightarrow dijets



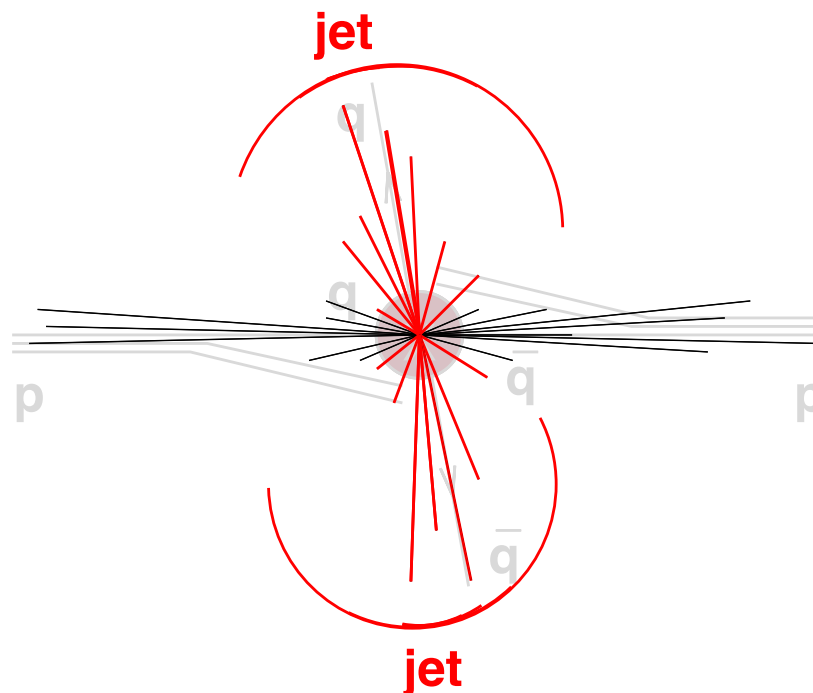
Resonance peak various R

R = 1.2

qq, M = 100 GeV



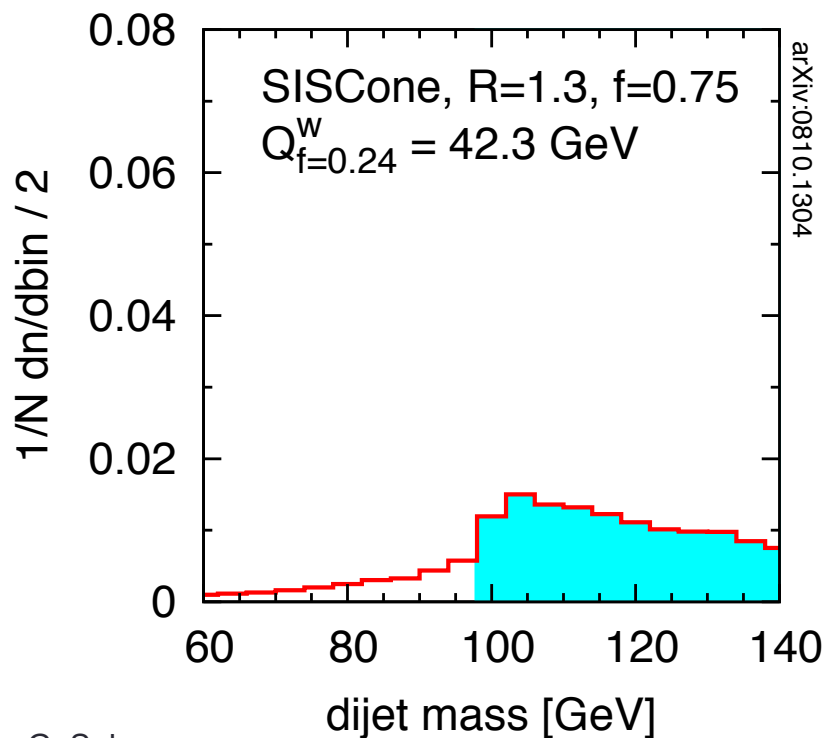
Resonance X \rightarrow dijets



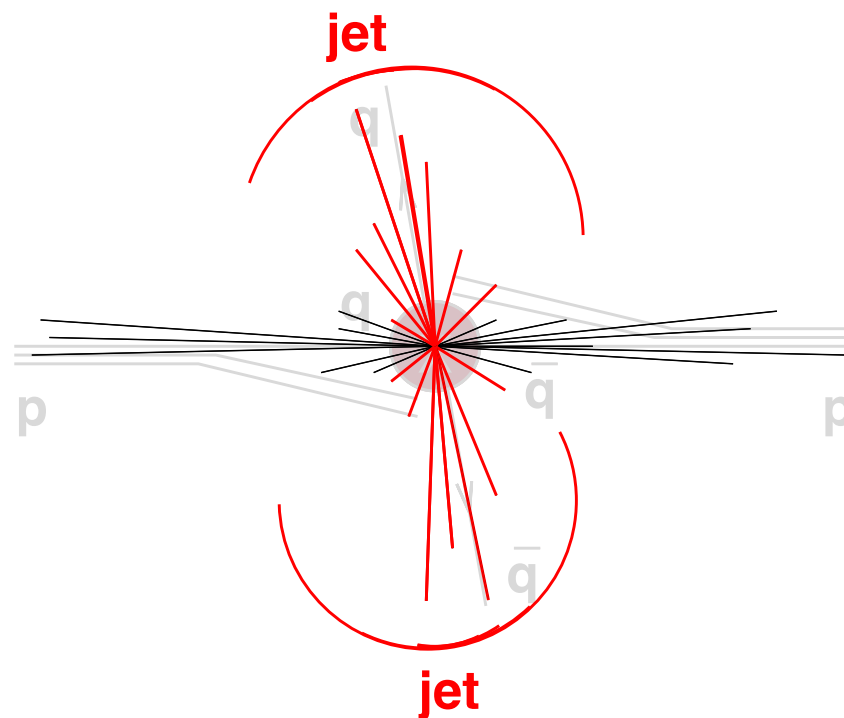
Resonance peak various R

$R = 1.3$

qq , $M = 100$ GeV



Resonance $X \rightarrow$ dijets

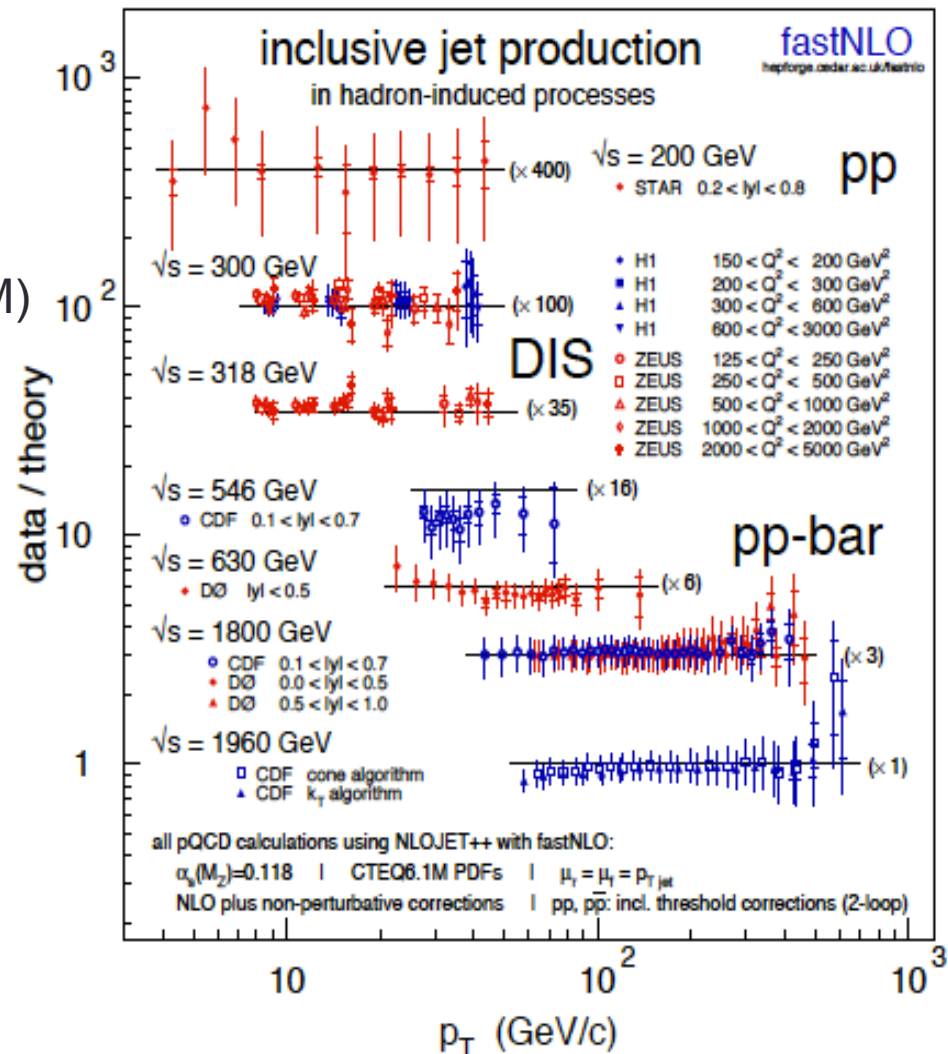
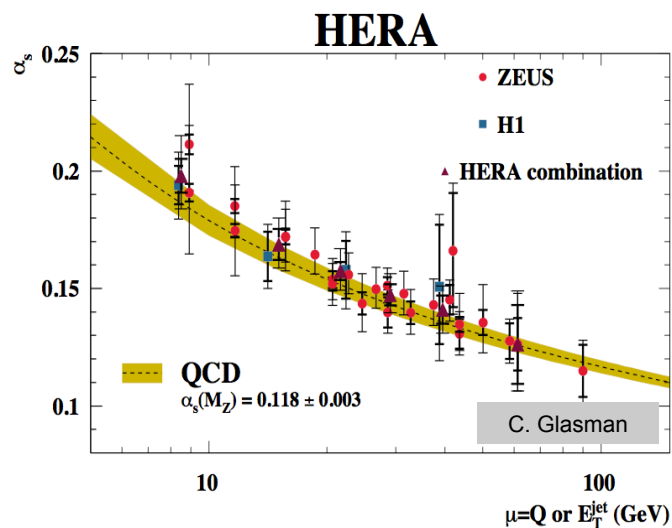


DATA

RHIC, Hera and Tevatron

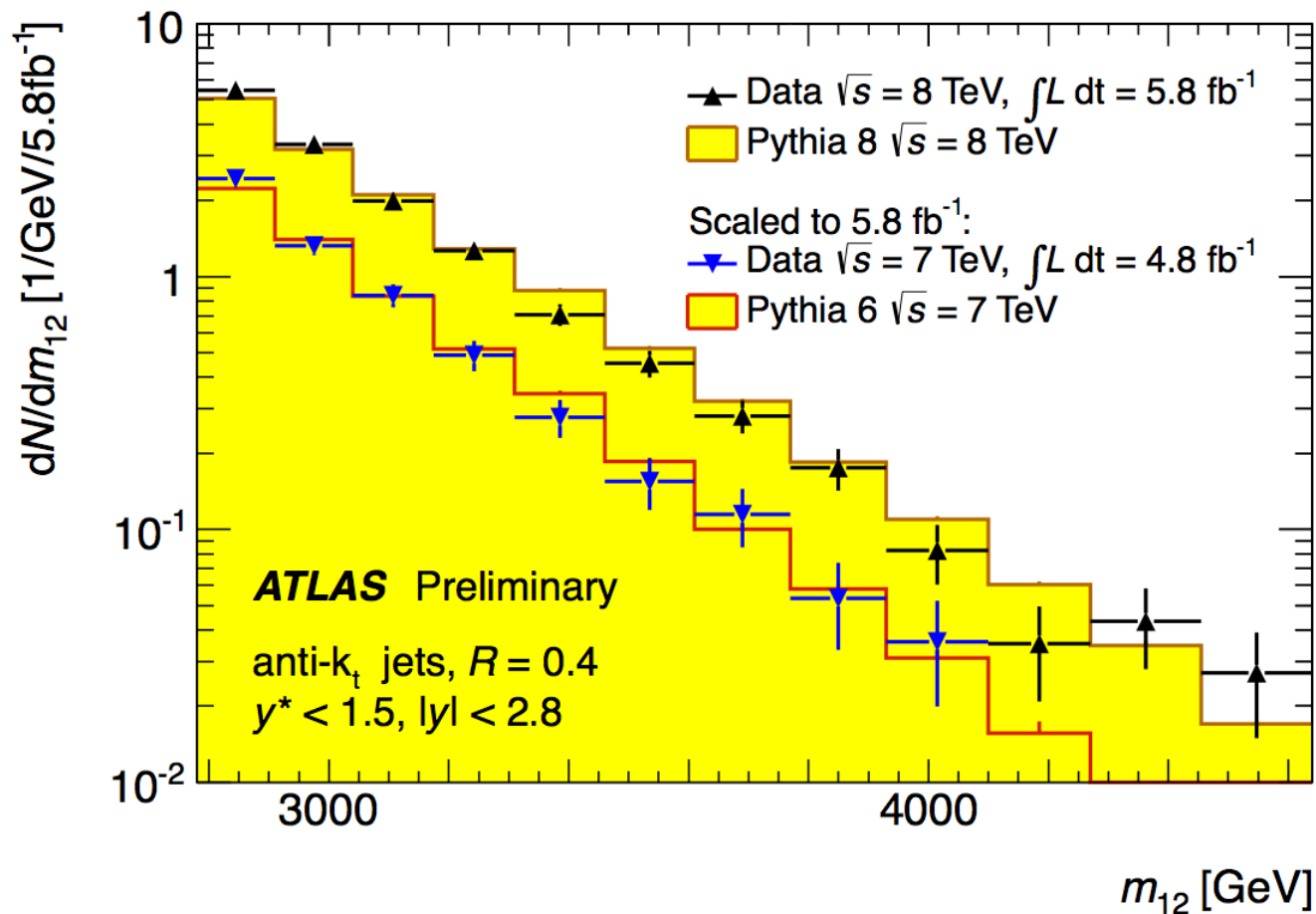
- Excellent agreement between NLO theory and data (10% level)
- Using same PDF set (CTEQ6.1M) and same

$$\alpha_s(m_Z) = 0.118$$

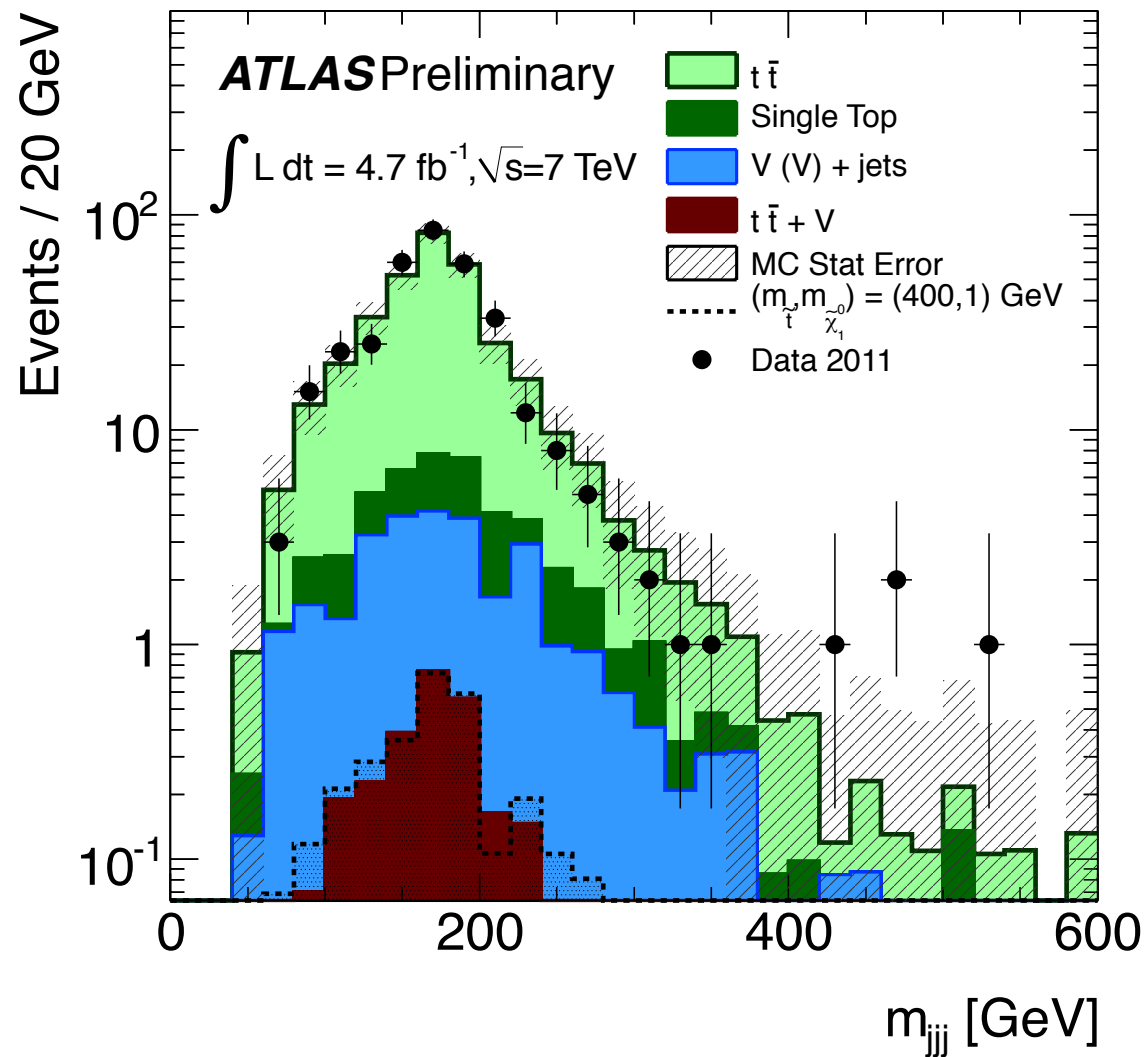


LHC data: dijet invariant mass

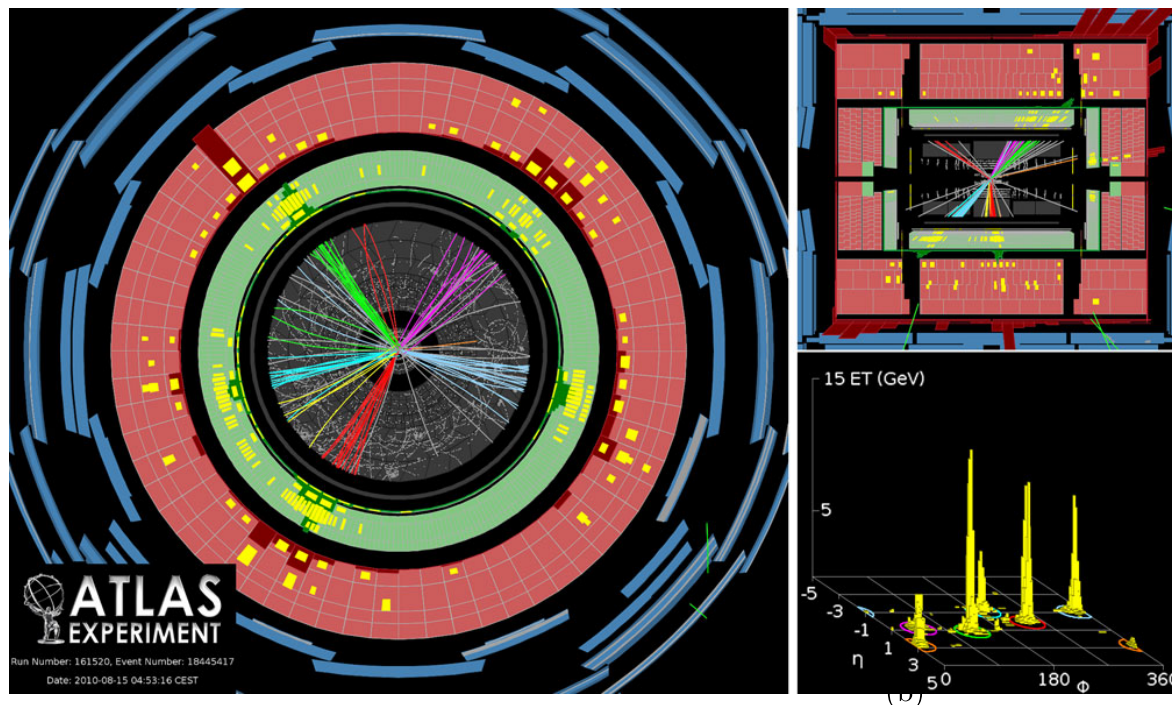
Atlas dijet invariant mass (anti- k_T $R=0.4$)



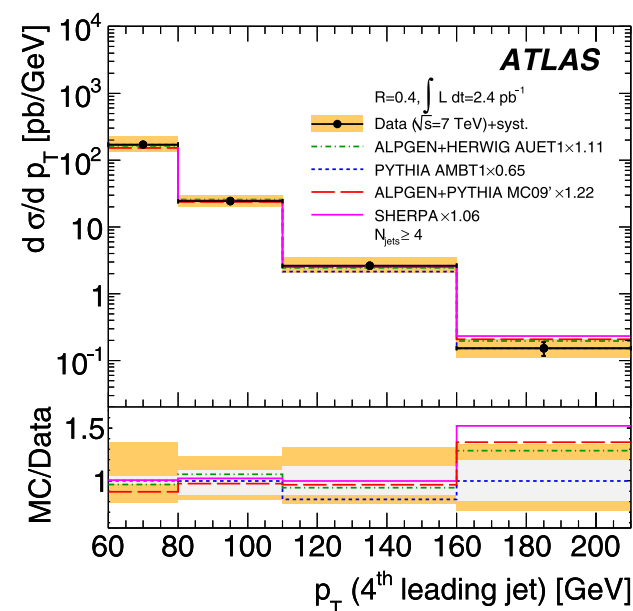
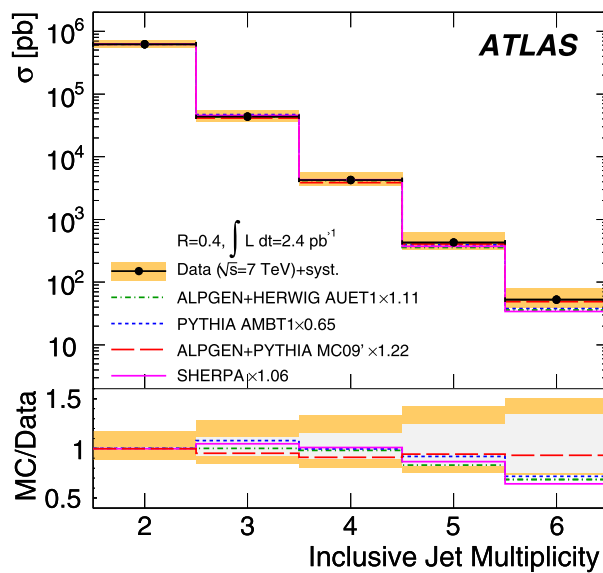
Tri-jet invariant mass



Multijets

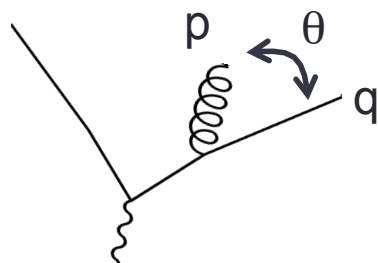
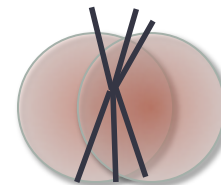


Multijet data
Agrees very well
with theory



Summary

- Jets exist because QCD is weakly coupled at short distances and strongly coupled at long distances
- Collinear and soft regions dominate cross sections



$$d\sigma = e^{-\int dP} dP$$

$$\sim e^{-\alpha \ln^2\left(\frac{\mu_1}{\mu_2}\right)} \left(\frac{\alpha_s}{2\pi} \frac{1+z}{1-z^2} \right) dz$$

- Semi-classical approximation “Sudakov factors and splitting-functions” works excellently
- Jet algorithms reconstruct parton momenta from jets

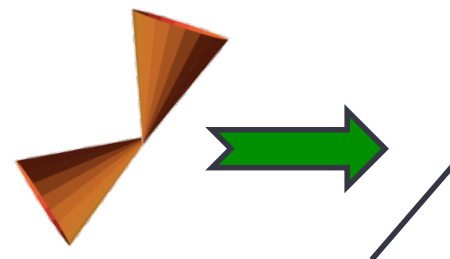
- Different algorithms

Cone algorithms
Cambridge/Aachen
 k_T
Anti- k_T



- Different goals

Reconstruct parton momenta
Infrared safe
Insensitive to pileup
Easy to calibrate experimentally



- Excellent agreement of theory with data